

Education Bureau
Territory-wide System Assessment 2010
Secondary 3 Mathematics
Marking Scheme

Note (for Section B and C of each sub-paper):

*Mark for Answer:

- (1) The Mark for Answer may be given when there is a correct answer without any work shown.
- (2) If the work shown is incorrect, the Mark for Answer will not be given.
- (3) If the work shown is poorly presented but there is a correct answer, the Mark for Answer may be given.

**Mark for Presentation:

- (1) If the work shown is correct but the answer is incorrect, the Mark for Presentation may be given.
- (2) If the work shown is incorrect, the Mark for Presentation will not be given.
- (3) If the numerical value of the answer is correct but not the approximate value as required by the question, the Mark for Presentation will not be given.
- (4) The Mark for Presentation may include overall work such as mathematical expressions, units, written explanations, usage of symbol, etc.

r.t. xxx means “accept answers which can be rounded to xxx ” .


Steps that may be skipped are shown in shade.

Alternative suggested answers are shown in boxes.

Section A – Sub-paper 1 (9ME1) (1 mark each)

1. B (9ME2-1)
2. D (9ME2-2)
3. D (9ME4-2)
4. C
5. B
6. A
7. A
8. C
9. D
10. C
11. D (9ME2-11)
12. A (9ME2-12)
13. A (9ME4-12)
14. B
15. A
16. D
17. C
18. B
19. C
20. B

Section B – Sub-paper 1 (9ME1)

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------|---|----------------------------------|----------------------|
| 21. (i) (ii) (9ME2-21) | -7 $+32$ / $\boxed{32}$ | Must be all correct | 1 |
| 22. (9ME2-22) | 36 / $\boxed{+36}$ | | 1 |
| 23. (9ME4-22) | (i) Estimated value (ii) Estimated value | Must be all correct | 1 |
| 24. | 148 | | 1 |
| 25. | 15 | | 1 |
| 26. | $(2x-1)^2$ / $\boxed{(2x-1)(2x-1)}$ | Factorization | 1 |
| 27. | $(x-5)(x-2)$ | Factorization | 1 |
| 28. | 7 | | 1 |
| 29. | $\frac{3y}{2x}$ | In simplest form | 1 |
| 30. (9ME2-30) | $\frac{y}{1-y}$ | Give mark if 'x=' is written | 1 |
| 31. (9ME2-31) | $x \geq 3$ | | 1 |
| 32. (9ME4-32) | $\angle VME$ / $\boxed{\angle EMV}$ | | 1 |
| 33. |  | The cross-section is a rectangle | 1 |
| 34. | 3 | | 1 |
| 35. | 110 | | 1 |
| 36. | $BCEF$ or its correct permutation, or $CDFG$ or its correct permutation, or $ABHE$ or its correct permutation, or $ACHF$ or its correct permutation, or $BDEG$ or its correct permutation. (ANY TWO) | 1 mark for each correct plane | 1 (36-1) 1 (36-2) |

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------|----------------------------------|-------------------------|-------|
| 37. | $A \cdot B$ | | 1 |
| 38. | $(4, -1)$ | | 1 |
| 39. | 56.3° | The unit can be omitted | 1 |
| 40. (9ME2-40) | 48 | | 1 |
| 41. (i) (ii) (9ME2-41) | Discrete data Continuous data | Must be all correct | 1 |
| 42. (9ME4-41) | 62 000 | | 1 |
| 43. | 6.7 | | 1 |

Section C – Sub-paper 1 (9ME1)

| Question Number | Suggested Answers | Marks | Notes |
|------------------|--|--|--|
| 44. (9ME4-44) | Area of the football field $= 40 \times 40 \times \frac{5}{2}$ $= 4000 \text{ m}^2$ | 1 (44-1) 1* (44-2) 1** (44-3) | For $40 \times \frac{5}{2} \times a$ or $100 \times a$, where a is a positive real number If only the length (100 m) is calculated, no marks will be given. |
| 45. (9ME4-45) | $\frac{x^{-2}}{(y^2)^3}$ $= \frac{x^{-2}}{y^{2 \times 3}}$ $= \frac{1}{x^{-(-2)} y^6}$ $= \frac{1}{x^2 y^6}$ | 1 (45-1) | Using $(y^m)^n = y^{mn}$ |
| | | 1 (45-2) | Using $\frac{1}{x^{-k}} = x^k$ or $x^{-k} = \frac{1}{x^{(-k)}}$ |
| | | 1* (45-3) | Correct answer (getting marks 1, 1, 1) |
| 46. | $\begin{cases} 3x + y = 70 & \dots(1) \\ y = 2x - 30 & \dots(2) \end{cases}$ Substitute (2) into (1) $3x + 2x - 30 = 70$ $x = 20$ Substitute $x = 20$ into (2) $y = 2(20) - 30$ $y = 10$ | 1 (46-1) 1* (46-2) 1 (46-3) 1* (46-4) | Method (eliminating one of the variables) First correct root (either x or y) Method (e.g. using the value of the first root to get the second root) Both roots are the correct answers |
| 47. (a) | Area of the small circle = $3^2 \pi$ $= 9\pi \text{ cm}^2$ | 1 (47a-1) 1* (47a-2) | Use correct method to find either one of the areas Express the answer in terms of π |
| (b) | Area of the large circle = $4^2 \pi$ $= 16\pi \text{ cm}^2$ | 1* (47a-3) | Express the answer in terms of π |
| | The shaded area = $16\pi - 9\pi$ $= 7\pi \text{ cm}^2$ | 1* (47b) | Express the answer in terms of π |
| | The shaded area is $7\pi \text{ cm}^2$ ◦ | 1** (47-4) | |

| Question Number | Suggested Answers | | Marks | Notes | | | | | | | | | | |
|---|---|---|--|--|------|---|------|---|------|----|------|----|--|---|
| 48. | $\angle KAC = \angle KBD$ $\angle KCA = \angle KDB$ $\angle AKC = \angle BKD$ $\therefore \triangle ACK \sim \triangle BDK$ | alt. \angle s, $PQ \parallel RS$ | 3 | Any correct proof with correct reasons | | | | | | | | | | |
| | | alt. \angle s, $PQ \parallel RS$ | 2 | Any correct proof without reasons or having wrong symbol | | | | | | | | | | |
| | | vert. opp. \angle s | 1 | Incomplete proof with any one correct statement and one corresponding reason | | | | | | | | | | |
| | | AAA / equiangular | 0 | Incomplete proof | | | | | | | | | | |
| | Alternative solution (1) | | Alternative solution (2) | | | | | | | | | | | |
| $\angle KAC = \angle KBD$ $\angle KCA = \angle KDB$ $\therefore \triangle ACK \sim \triangle BDK$ | alt. \angle s, $PQ \parallel RS$ alt. \angle s, $PQ \parallel RS$ AA | $\angle KAC = \angle KBD$ / $\angle KCA = \angle KDB$ $\angle AKC = \angle BKD$ $\therefore \triangle ACK \sim \triangle BDK$ | alt. \angle s, $PQ \parallel RS$ / alt. \angles, $PQ \parallel RS$ vert. opp. \angle s AA | | | | | | | | | | | |
| 49. | $\cos 34^\circ = \frac{AB}{800}$ $AB \approx 663.230058$ $AB = 663.2$ (corr. to 1 d.p.) The horizontal distance between these two stations is 663.2 m. | | 1 (49-1) 1* (49-2) 1** (49-3) | Related and correct set up r.t. 663.2 | | | | | | | | | | |
| 50. | <p style="text-align: center;">The ages of 40 staff in Tai Tai Fast Food Shop</p> <table border="1" style="margin-top: 10px; width: 100%; text-align: center;"> <caption>Data from Histogram</caption> <thead> <tr> <th>Age Class</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>25.5</td> <td>6</td> </tr> <tr> <td>35.5</td> <td>8</td> </tr> <tr> <td>45.5</td> <td>14</td> </tr> <tr> <td>55.5</td> <td>12</td> </tr> </tbody> </table> | | Age Class | Frequency | 25.5 | 6 | 35.5 | 8 | 45.5 | 14 | 55.5 | 12 | 1 (50-1) 1 (50-2) 1 (50-3) | The class marks match with the corresponding frequencies (6, 8, 14, 12) 2 class marks are correct (45.5, 55.5) Correct histogram (No marks will be given if any charts other than histogram are also shown as well) |
| Age Class | Frequency | | | | | | | | | | | | | |
| 25.5 | 6 | | | | | | | | | | | | | |
| 35.5 | 8 | | | | | | | | | | | | | |
| 45.5 | 14 | | | | | | | | | | | | | |
| 55.5 | 12 | | | | | | | | | | | | | |

| Question Number | Suggested Answers | Marks | Notes |
|-------------------|---|--|---|
| 51. (9ME2-52). | (Students should estimate the prices of gifts so as to find the number of gifts. The total costs cannot exceed \$70.) For example : $9.8 \times 5 + 18.9 \times 1$ $\approx 10 \times 5 + 20 \times 1$ $= 70$ \therefore Terence can buy 6 gifts. | 0 (51-1) 0 (51-2) No evidence of using estimation strategy and giving reasonable justification | <ul style="list-style-type: none"> ◆ Give estimate only after exact calculation ◆ Wrong estimation (e.g. $29.4 \approx 29$) ◆ Exact calculation only ◆ Give an estimate and only one kind of gifts is bought |
| | Possible answers : (a) $9.8 \times 5 + 18.9 \times 1 \approx 10 \times 5 + 20 \times 1 = 70$ \therefore Terence can buy 6 gifts. (b) $9.8 \times 4 + 29.4 \times 1 \approx 10 \times 4 + 30 \times 1 = 70$ \therefore Terence can buy 5 gifts. (c) $9.8 \times 3 + 18.9 \times 2 \approx 10 \times 3 + 20 \times 2 = 70$ \therefore Terence can buy 5 gifts. (d) $9.8 \times 2 + 29.4 \times 1 + 18.9 \times 1$ $\approx 10 \times 2 + 30 \times 1 + 20 \times 1 = 70$ \therefore Terence can buy 4 gifts. (e) $9.8 \times 1 + 29.4 \times 2 \approx 10 \times 1 + 30 \times 2 = 70$ \therefore Terence can buy 3 gifts. | 1 (51-1) 0 (51-2) Partial evidence of using estimation strategy, but the solution is incomplete or contains errors | <ul style="list-style-type: none"> ◆ Correct estimation (e.g. 10, 19/20, 30) ◆ Estimate correctly, but only one kind of gift is bought ◆ Estimate correctly, but the total costs is greater than \$70 or not greater than \$60 ◆ Estimation by using correct method, but minor error occurred |
| | (f) $9.8 \times 1 + 18.9 \times 3 \approx 10 \times 1 + 20 \times 3 = 70$ \therefore Terence can buy 4 gifts. (g) $18.9 \times 2 + 29.4 \times 1 \approx 20 \times 2 + 30 \times 1 = 70$ \therefore Terence can buy 3 gifts. | 1 (51-1) 1 (51-2) Estimate with reasonable justification | <ul style="list-style-type: none"> ◆ No need to consider unit/presentation ◆ Accept using '\leq' instead of '\approx' |

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****Mark for Presentation:**

- (1) If the work shown is correct but the answer is incorrect, the Mark for Presentation may be given.
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- (4) The Mark for Presentation may include overall work such as mathematical expressions, units, written explanations, usage of symbol, etc.

r.t. xxx means “accept answers which can be rounded to xxx ” .

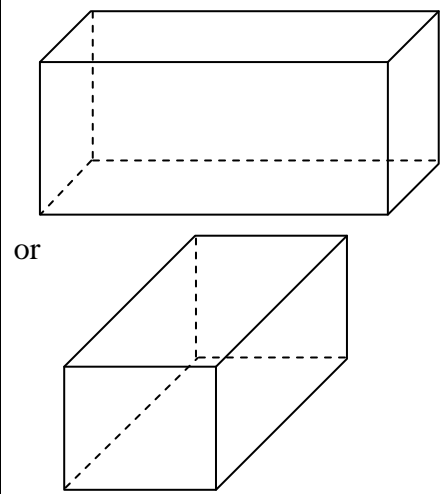
Steps that may be skipped are shown in shade.

Alternative suggested answers are shown in boxes.

Section A – Sub-paper 2 (9ME2) (1 mark each)

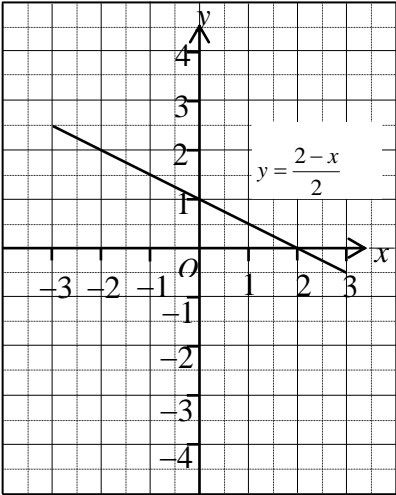
1. B (9ME1-1)
2. D (9ME1-2)
3. C (9ME3-2)
4. B (9ME3-3)
5. B (9ME4-4)
6. A
7. C
8. D
9. A
10. C
11. D (9ME1-11)
12. A (9ME1-12)
13. B (9ME3-12)
14. D (9ME3-13)
15. C (9ME4-14)
16. A
17. C
18. A
19. D
20. B

Section B – Sub-paper 2 (9ME2)

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------|--|--|-------|
| 21. (i) (ii) (9ME1-21) | -7 $+32$ / $\boxed{32}$ | Must be all correct | 1 |
| 22. (9ME1-22) | 36 / $\boxed{+36}$ | | 1 |
| 23. (9ME3-22) | 20 | | 1 |
| 24. (9ME4-24) | 63 | | 1 |
| 25. | 5 及 $-\frac{5}{2}$ / $\boxed{-2.5}$ | Must be all correct | 1 |
| 26. | 6 | | 1 |
| 27. | $3ab(3b - 5a)$ | Factorization | 1 |
| 28. | Q and S / $\boxed{Q, S}$ / $\boxed{Q(-2, 3) \text{ and } S(2, 0)}$ / $\boxed{Q(-2, 3), S(2, 0)}$ | Must be all correct | 1 |
| 29. | $x^2 - 4y^2$ | Expansion | 1 |
| 30. (9ME1-30) | $\frac{y}{1-y}$ | Give mark if 'x=' is written | 1 |
| 31. (9ME1-31) | $x \geq 3$ | | 1 |
| 32. (9ME3-30) | 3 | | 1 |
| 33. (i) (ii) (9ME3-31) | volume surface area | Must be all correct | 1 |
| 34. (9ME4-34) |  | <p>Or other correct cuboids</p> <p>Must use solid lines and dotted lines to show all edges</p> | 1 |

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------------|--|-------------------------|-------------------------------|
| 35. | A、C | Must be all correct | 1 |
| 36. | 113° | The unit can be omitted | 1 |
| 37. | 3.9 | | 1 |
| 38. | 20 | | 1 |
| 39. | 56 | | 1 |
| 40. (9ME1-40) | 48 | | 1 |
| 41. (i) (ii) (9ME1-41) | Discrete data Continuous data | Must be all correct | 1 |
| 42. (a) (b) (c) (9ME3-40) | 15:00 / 3:00 p.m. 4.4 12:00 / noon | 3:00 is not accepted | 1 (42a) 1 (42b) 1 (42c) |
| 43. (9ME3-41) | 3 | | 1 |

Section C – Sub-paper 2 (9ME2)

| Question Number | Suggested Answers | Marks | Notes | | | | | | | | |
|--------------------|---|--|--|---|---|-----|---|---|---|---|--|
| 44. (a) (b) | Interest = $3270 - 3000$ = \$270 Annual interest rate = $270 \div 3 \div 3000$ = 0.03 = 3% | 1* (44a) 1 (44b-1) 1* (44b-2) 1** (44-3) | | | | | | | | | |
| 45. (9ME3-44) | $20000 \times (1 - 20\%)^3$ = \$10240 The value of the machine after three years is \$10240. OR $20000 \times 0.8 = 16000$ $16000 \times 0.8 = 12800$ $12800 \times 0.8 = 10240$ The value of the machine after three years is \$10240. | 1 (45-1) 1* (45-2) 1** (45-3) $\boxed{1}$ (45-1) $\boxed{1^*}$ (45-2) $\boxed{1^{**}}$ (45-3) | Set up $\boxed{\text{Correct method (multiply 0.8 three times)}}$ | | | | | | | | |
| 46. (9ME3-45) | Water consumed by factory $= \frac{1}{1.31} \times 5240$ $= 4000 \text{ m}^3$ | 1 (46-1) 1* (46-2) 1** (46-3) | Or other correct methods | | | | | | | | |
| 47. (9ME4-46) | <table border="1" style="margin-bottom: 10px;"> <tr> <td>x</td> <td>-2</td> <td>0</td> <td>2</td> </tr> <tr> <td>y</td> <td>2</td> <td>1</td> <td>0</td> </tr> </table>  | x | -2 | 0 | 2 | y | 2 | 1 | 0 | 1 (47-1) 1 (47-2) 1* (47-3) | Must be all correct In case the data in the above table is incorrect, student can still use the ordered pairs to draw a straight line. The line must pass through (0, 1) and the range of value of x must include -2 to 2 . Correct straight line (include: correct position, use ruler to draw the line, pass through the 3 points and extend in two ends of the line) If the data in the table is correct but not complete and the graph is correct, (0, 1, 1) can be given |
| x | -2 | 0 | 2 | | | | | | | | |
| y | 2 | 1 | 0 | | | | | | | | |

| Question Number | Suggested Answers | Marks | Notes | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--------------------------|--|--|---|--|-----------|-------|---|--------|---|---------|---|---------|---|---------|---|---------|---|---------|--|--------------------------|-----------|--------|---|---------|---|---------|---|---------|---|--|--|
| 48. | The area of the sector $= \left(\frac{145^\circ}{360^\circ}\right)\pi(16^2)$ ≈ 323.9331092 $= 323.9 \text{ cm}^2 \text{ (Corr. to the nearest } 0.1 \text{ cm}^2)$ | 1 (48-1) 1* (48-2) 1** (48-3) | r.t. 323.9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 49. | $x + x + 70^\circ = 180^\circ$ $\therefore x = 55^\circ$ $y + 30^\circ = 70^\circ$ $\therefore y = 40^\circ$ | 1 (49-1) 1* (49-2) 1* (49-3) | Using correct method to find either x or y | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | Alternative solution (1) | | Alternative solution (2) | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | $x + x + 70^\circ = 180^\circ$ $\therefore x = 55^\circ$ $\angle BDC + 70^\circ = 180^\circ$ $\angle BDC = 110^\circ$ $30^\circ + \angle BDC + y = 180^\circ$ $\therefore y = 40^\circ$ | 1 (49-1) 1* (49-2) 1* (49-3) | $x + x + 70^\circ = 180^\circ$ $\therefore x = 55^\circ$ $x + (x + 30^\circ) + y = 180^\circ$ $55^\circ + 55^\circ + 30^\circ + y = 180^\circ$ $\therefore y = 40^\circ$ 1* (49-3) | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50. | $AB = AC$ $BD = CD$ $AD = AD$ $\therefore \triangle ABD \cong \triangle ACD$ | given given common side SSS | 3 2 1 0 | Any correct proof with correct reasons Any correct proof without reasons or having wrong symbol Incomplete proof with any one correct statement and one corresponding reason Incomplete proof | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 51. (9ME4-48) | <table border="1" style="width: 100%; text-align: center;"> <thead> <tr> <th colspan="2">Table 1</th> </tr> <tr> <th>Number of books borrowed</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>1 – 8</td> <td>4</td> </tr> <tr> <td>9 – 16</td> <td>5</td> </tr> <tr> <td>17 – 24</td> <td>4</td> </tr> <tr> <td>25 – 32</td> <td>3</td> </tr> <tr> <td>33 – 40</td> <td>2</td> </tr> <tr> <td>41 – 48</td> <td>2</td> </tr> </tbody> </table> <table border="1" style="width: 100%; text-align: center;"> <thead> <tr> <th colspan="2">Table 2</th> </tr> <tr> <th>Number of books borrowed</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>1 – 12</td> <td>6</td> </tr> <tr> <td>13 – 24</td> <td>7</td> </tr> <tr> <td>25 – 36</td> <td>5</td> </tr> <tr> <td>37 – 48</td> <td>2</td> </tr> </tbody> </table> | Table 1 | | Number of books borrowed | Frequency | 1 – 8 | 4 | 9 – 16 | 5 | 17 – 24 | 4 | 25 – 32 | 3 | 33 – 40 | 2 | 41 – 48 | 2 | Table 2 | | Number of books borrowed | Frequency | 1 – 12 | 6 | 13 – 24 | 7 | 25 – 36 | 5 | 37 – 48 | 2 | 1 (51-1) 1 (51-2) | Must be all correct Must be all correct |
| Table 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Number of books borrowed | Frequency | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 – 8 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 9 – 16 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 17 – 24 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 – 32 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 33 – 40 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 41 – 48 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Table 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Number of books borrowed | Frequency | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 – 12 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 13 – 24 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 – 36 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 37 – 48 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Question Number | Suggested Answers | Marks | Notes |
|------------------|--|--|---|
| 52. (9ME1-51) | (Students should estimate the prices of gifts so as to find the number of gifts. The total costs cannot exceed \$70.) For example : $9.8 \times 5 + 18.9 \times 1$ $\approx 10 \times 5 + 20 \times 1$ $= 70$ \therefore Terence can buy 6 gifts. | 0 (52-1) 0 (52-2) No evidence of using estimation strategy and giving reasonable justification | <ul style="list-style-type: none"> ◆ Give estimate only after exact calculation ◆ Wrong estimation (e.g. $29.4 \approx 29$) ◆ Exact calculation only ◆ Give an estimate and only one kind of gifts is bought |
| | Possible answers : (a) $9.8 \times 5 + 18.9 \times 1 \approx 10 \times 5 + 20 \times 1 = 70$ \therefore Terence can buy 6 gifts. (b) $9.8 \times 4 + 29.4 \times 1 \approx 10 \times 4 + 30 \times 1 = 70$ \therefore Terence can buy 5 gifts. (c) $9.8 \times 3 + 18.9 \times 2 \approx 10 \times 3 + 20 \times 2 = 70$ \therefore Terence can buy 5 gifts. (d) $9.8 \times 2 + 29.4 \times 1 + 18.9 \times 1$ $\approx 10 \times 2 + 30 \times 1 + 20 \times 1 = 70$ \therefore Terence can buy 4 gifts. (e) $9.8 \times 1 + 29.4 \times 2 \approx 10 \times 1 + 30 \times 2 = 70$ \therefore Terence can buy 3 gifts. (f) $9.8 \times 1 + 18.9 \times 3 \approx 10 \times 1 + 20 \times 3 = 70$ \therefore Terence can buy 4 gifts. (g) $18.9 \times 2 + 29.4 \times 1 \approx 20 \times 2 + 30 \times 1 = 70$ \therefore Terence can buy 3 gifts. | 1 (52-1) 0 (52-2) Partial evidence of using estimation strategy, but the solution is incomplete or contains errors | <ul style="list-style-type: none"> ◆ Correct estimation (e.g. 10, 19/20, 30) ◆ Estimate correctly, but only one kind of gift is bought ◆ Estimate correctly, but the total costs is greater than \$70 or not greater than \$60 ◆ Estimation by using correct method, but minor error occurred |
| | | 1 (52-1) 1 (52-2) Estimate with reasonable justification | <ul style="list-style-type: none"> ◆ No need to consider unit/presentation ◆ Accept using '\leq' instead of '\approx' |

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r.t. xxx means “accept answers which can be rounded to xxx ” .

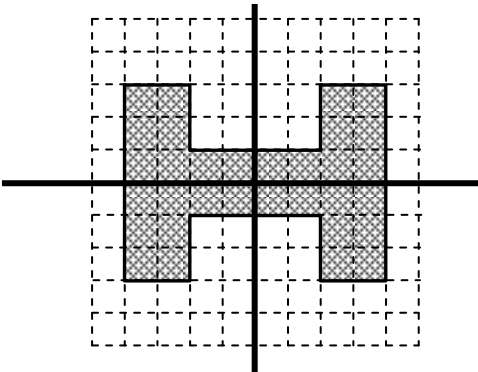
Steps that may be skipped are shown in shade.

Alternative suggested answers are shown in boxes.

Section A – Sub-paper 3 (9ME3) (1 mark each)

1. D
2. C (9ME2-3)
3. B (9ME2-4)
4. A
5. D (9ME4-5)
6. A
7. B
8. C
9. A
10. C
11. B
12. B (9ME2-13)
13. D (9ME2-14)
14. A
15. C (9ME4-15)
16. D
17. C
18. B
19. A (9ME4-19)
20. D

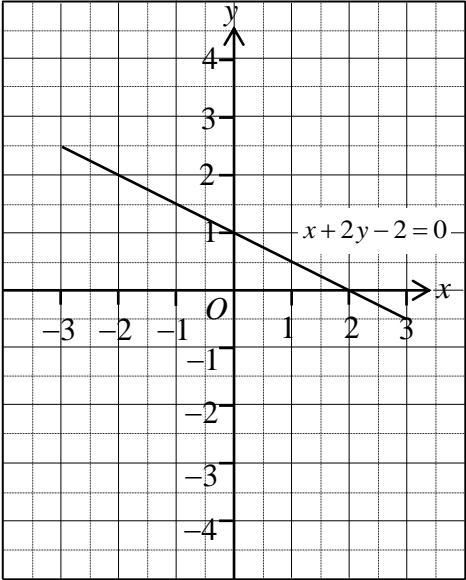
Section B – Sub-paper 3 (9ME3)

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------|---|------------------------|-------|
| 21. | $A = -2$ $B = 0$ $C = 6$ $C = +6$ | Must be all correct | 1 |
| 22. (9ME2-23) | 20 | | 1 |
| 23. | $4 : 5$ / $0.8 : 1$ / $1 : 1.25$ / $\frac{4}{5} : 1$ / $1 : \frac{5}{4}$ / $\frac{4}{5}$ | | 1 |
| 24. (9ME4-25) | $3x < A$ / $3x - A < 0$ | Not accept $3x \leq A$ | 1 |
| 25. | 3^n | | 1 |
| 26. | $2x^2 + 3x - 2$ | Expansion | 1 |
| 27. | $(2x - 3)(2x + 3)$ | Factorization | 1 |
| 28. | 5 | | 1 |
| 29. (i) | $\frac{3}{4}$ <input type="text" value="<"/> $\frac{3}{2}$ | Must be all correct | 1 |
| (ii) | $-\frac{3}{4}$ <input type="text" value=">"/> $-\frac{3}{2}$ | | |
| 30. (9ME2-32) | 3 | | 1 |
| 31. (i) (ii) (9ME2-33) | volume surface area | Must be all correct | 1 |
| 32. | C、D | Must be all correct | 1 |
| 33. (9ME4-35) |  | | 1 |
| 34. | 60 | | 1 |
| 35. | $2x^3 - 6x^2 + 2x$ | Expansion | 1 |
| 36. | BD / DB | | 1 |
| 37. | (1, 3) | | 1 |

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------------|--|--|-------------------------------|
| 38. | 26 | | 1 |
| 39. | (2) → (4) → (1) → (3) | | 1 |
| 40. (a) (b) (c) (9ME2-42) | 15:00 / 3:00 p.m. 4.4 12:00 / noon | 3:00 is not accepted | 1 (40a) 1 (40b) 1 (40c) |
| 41. (9ME2-43) | 3 | | 1 |
| 42. | 0.26 / $\frac{13}{50}$ | Need simplification $\frac{52}{200}$ no mark will be given | 1 |

Section C – Sub-paper 3 (9ME3)

| Question Number | Suggested Answers | Marks | Notes |
|--------------------|---|--|---|
| 43. (a) (b) | $\text{Amount} = 25000 \times (1 + 4\%)^2$ $= \$27040$ $\text{Interest} = 27040 - 25000$ $= \$2040$ | 1 (43a-1) 1* (43a-2) 1* (43b) 1** (43-3) | Set up |
| 44. (9ME2-45) | $20000 \times (1 - 20\%)^3$ $= \$10240$ <p>The value of the machine after three years is \$10240.</p> <p>OR</p> <div style="border: 1px solid black; padding: 2px; width: fit-content;"> $20000 \times 0.8 = 16000$ </div> <div style="border: 1px solid black; padding: 2px; width: fit-content;"> $16000 \times 0.8 = 12800$ </div> <div style="border: 1px solid black; padding: 2px; width: fit-content;"> $12800 \times 0.8 = 10240$ </div> <div style="border: 1px solid black; padding: 2px; width: fit-content;"> <p>The value of the machine after three years is \$10240.</p> </div> | 1 (44-1) 1* (44-2) 1** (44-3) <div style="border: 1px solid black; padding: 2px; width: fit-content;"> 1 (44-1) </div> <div style="border: 1px solid black; padding: 2px; width: fit-content;"> 1* (44-2) </div> <div style="border: 1px solid black; padding: 2px; width: fit-content;"> 1** (44-3) </div> | Set up <div style="border: 1px solid black; padding: 2px; width: fit-content;"> Correct method (multiply 0.8 three times) </div> |
| 45. (9ME2-46) | <p>Water consumed by Rainbow factory</p> $= \frac{1}{1.31} \times 5240$ $= 4000 \text{ m}^3$ | 1 (45-1) 1* (45-2) 1** (45-3) | Or other correct methods |

| Question Number | Suggested Answers | Marks | Notes | | | | | | | | |
|-----------------|--|--|--|---|---|---|---|---|---|--|--|
| 46. | <table border="1" data-bbox="352 315 722 414"> <tr> <td>x</td> <td>-2</td> <td>0</td> <td>2</td> </tr> <tr> <td>y</td> <td>2</td> <td>1</td> <td>0</td> </tr> </table>  | x | -2 | 0 | 2 | y | 2 | 1 | 0 | <p>1 (46-1)</p> <p>1 (46-2)</p> <p>1* (46-3)</p> | <p>Must be all correct</p> <p>In case the data in the above table is incorrect, student can still use the ordered pairs to draw a straight line. The line must pass through (0, 1) and the range of value of x must include -2 to 2.</p> <p>Correct straight line (include: correct position, use ruler to draw the line, pass through the 3 points and extend in two ends of the line)</p> <p>If the data in the table is correct but not complete and the graph is correct, (0, 1, 1) can be given</p> |
| x | -2 | 0 | 2 | | | | | | | | |
| y | 2 | 1 | 0 | | | | | | | | |
| 47. | $V = 3^2 \times \pi \times (5 - 4)$ $= 9\pi$ | <p>1 (47-1)</p> <p>1* (47-2)</p> | <p>Or other correct methods</p> | | | | | | | | |
| 48. | <p>The volume of the sphere is</p> $\frac{4}{3}\pi\left(\frac{6}{2}\right)^3$ $= 36\pi \text{ cm}^3$ | <p>1 (48-1)</p> <p>1* (48-2)</p> <p>1** (48-3)</p> | | | | | | | | | |
| 49. | $\because AB = BC = CA$ $\therefore \angle ACB = 60^\circ$ $\because BC = DC$ $\therefore \angle CBD = \angle CDB = 35^\circ$ $(\angle ACD + 60^\circ) + 35^\circ + 35^\circ = 180^\circ$ $\therefore \angle ACD = 50^\circ$ | <p>1 (49-1)</p> <p>1 (49-2)</p> <p>1* (49-3)</p> | <p>For finding $\angle ACB = 60^\circ$ OR $\angle CDB = 35^\circ$; can be absorbed</p> <p>Or other correct methods</p> | | | | | | | | |

| Question Number | Suggested Answers | Marks | Notes |
|-----------------|---|--|--|
| 50. | $x + 70 + 70 = 180$ $x = 40$ | 1 (50-1) 1* (50-2) | Or other correct methods |
| 51. (a) (b) | Mode Disagree. There are only 2 months whose maximum relative humidity is 43% but the maximum relative humidities of other months (10 months) are higher than 43%. <div style="border: 1px solid black; padding: 2px;">There are only 2 months whose maximum</div> <div style="border: 1px solid black; padding: 2px;">relative humidity is 43% and lower than the</div> <div style="border: 1px solid black; padding: 2px;">maximum relative humidities of other months.</div> | 1 (51a) 1 (51b-1) 1 (51b-2) <div style="border: 1px solid black; padding: 2px;">1 (51b-2)</div> | Reasonable attempt to explain Explanation <div style="border: 1px solid black; padding: 2px;">Explanation</div> If 'agree' is chosen, the mark (0, 0) will be given to part (b) |

Education Bureau
Territory-wide System Assessment 2010
Secondary 3 Mathematics
Marking Scheme

Note (for Section B and C of each sub-paper):

*Mark for Answer:

- (1) The Mark for Answer may be given when there is a correct answer without any work shown.
- (2) If the work shown is incorrect, the Mark for Answer will not be given.
- (3) If the work shown is poorly presented but there is a correct answer, the Mark for Answer may be given.

**Mark for Presentation:

- (1) If the work shown is correct but the answer is incorrect, the Mark for Presentation may be given.
- (2) If the work shown is incorrect, the Mark for Presentation will not be given.
- (3) If the numerical value of the answer is correct but not the approximate value as required by the question, the Mark for Presentation will not be given.
- (4) The Mark for Presentation may include overall work such as mathematical expressions, units, written explanations, usage of symbol, etc.

r.t. xxx means “accept answers which can be rounded to xxx ” .

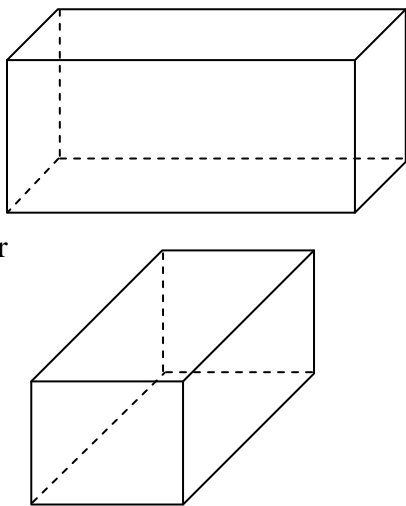
Steps that may be skipped are shown in shade.

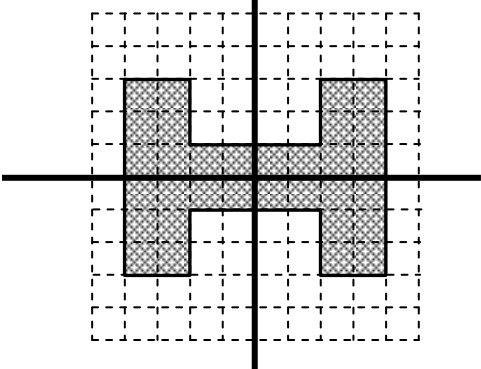
Alternative suggested answers are shown in boxes.

Section A – Sub-paper 4 (9ME4) (1 mark each)

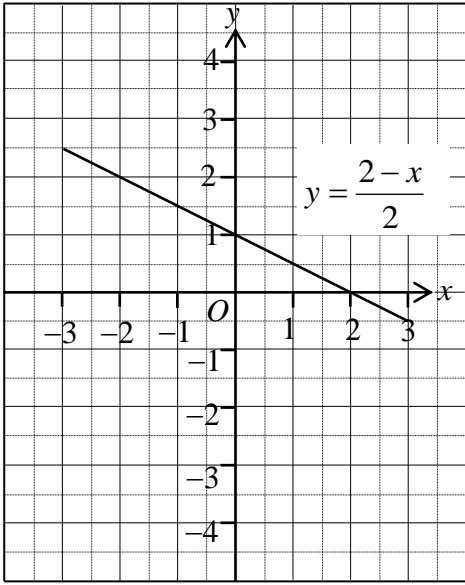
1. B
2. D (9ME1-3)
3. A
4. B (9ME2-5)
5. D (9ME3-5)
6. C
7. D
8. D
9. C
10. D
11. A
12. A (9ME1-13)
13. A
14. C (9ME2-15)
15. C (9ME3-15)
16. B
17. B
18. C
19. A (9ME3-19)
20. B

Section B – Sub-paper 4 (9ME4)

| Question Number | Suggested Answers | Notes | Marks |
|------------------------------|---|--|-------|
| 21. | -2 | | 1 |
| 22. (i) (ii) (9ME1-23) | Estimated value Estimated value | Must be all correct | 1 |
| 23. (i) (ii) | Ratio Rate | Must be all correct | 1 |
| 24. (9ME2-24) | 63 | | 1 |
| 25. (9ME3-24) | $3x < A$ / $3x - A < 0$ | Not accept $3x \leq A$ | 1 |
| 26. | 26 | | 1 |
| 27. | $a^2 + 4ab$ / $a(a + 4b)$ | Simplification | 1 |
| 28. | $x = 2, y = 1$ | Must be all correct | 1 |
| 29. | $4x^2 - 20x + 25$ | Expansion | 1 |
| 30. | $(2x - 1)(x + 3)$ | Factorization | 1 |
| 31. | $x > 8$ | | 1 |
| 32. (9ME1-32) | $\angle VME$ / $\angle EMV$ | | 1 |
| 33. | $\angle QSR$ / $\angle RSQ$ | | 1 |
| 34. (9ME2-34) |  <p>or</p> | <p>Or other correct cuboids</p> <p>Must use solid lines and dotted lines to show all edges</p> | 1 |

| Question Number | Suggested Answers | Notes | Marks |
|-----------------------|--|---|-------------------------------|
| 35. (9ME3-33) |  | | 1 |
| 36. (a) (b) | 66 10 | | 1 (36a) 1 (36b) |
| 37. | A, C / (A), (C) A 及 C / (A) 及 (C) / A 或 C / (A) 或 (C) / AC / (A)(C) / YZ, QT | Must be all correct | 1 |
| 38. | (2, 270°) | Must be all correct and in order | 1 |
| 39. | 5.5 | Reference value 5.45598688 r.t. 5.5 | 1 |
| 40. (a) (b) (c) | D 90 300 | | 1 (40a) 1 (40b) 1 (40c) |
| 41. (9ME1-42) | 62 000 | | 1 |
| 42. | 6 | | 1 |
| 43. | $\frac{3}{8}$ / 0.375 | | 1 |

Section C – Sub-paper 4 (9ME4)

| Question Number | Suggested Answers | Marks | Notes | | | | | | | | |
|------------------|--|---|---|---|---|-----|---|---|---|---|---|
| 44. (9ME1-44) | Area of the football field $= 40 \times 40 \times \frac{5}{2}$ $= 4000 \text{ m}^2$ | 1 (44-1) 1* (44-2) 1** (44-3) | For $40 \times \frac{5}{2} \times a$ or $100 \times a$, where a is a positive real number If only the length (100 m) is calculated, no marks will be given. | | | | | | | | |
| 45. (9ME1-45) | $\frac{x^{-2}}{(y^2)^3}$ | | | | | | | | | | |
| | $= \frac{x^{-2}}{y^{2 \times 3}}$ | 1 (45-1) | Using $(y^m)^n = y^{mn}$ | | | | | | | | |
| | $= \frac{1}{x^{-(-2)} y^6}$ | 1 (45-2) | Using $\frac{1}{x^{-k}} = x^k$ or $x^{-k} = \frac{1}{x^{-(-k)}}$ | | | | | | | | |
| | $= \frac{1}{x^2 y^6}$ | 1* (45-3) | Correct final answer (getting marks 1, 1, 1) | | | | | | | | |
| 46. (9ME2-47) | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td> <td>-2</td> <td>0</td> <td>2</td> </tr> <tr> <td>y</td> <td>2</td> <td>1</td> <td>0</td> </tr> </table>  | x | -2 | 0 | 2 | y | 2 | 1 | 0 | 1 (46-1) 1 (46-2) 1* (46-3) | Must be all correct In case the data in the above table is incorrect, student can still use the ordered pairs to draw a straight line. The line must pass through (0, 1) and the range of value of x must include -2 to 2. Correct straight line (include: correct position, use ruler to draw the line, pass through the 3 points and extend in two ends of the line) If the data in the table is correct but not complete and the graph is correct, (0, 1, 1) can be given |
| x | -2 | 0 | 2 | | | | | | | | |
| y | 2 | 1 | 0 | | | | | | | | |

| Question Number | Suggested Answers | Marks | Notes | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|--------------------------|--|--|---|--------------------------|-----------|-------|---|--------|---|---------|---|---------|---|---------|---|---------|---|---------|--|--------------------------|-----------|--------|---|---------|---|---------|---|---------|---|--|--|
| 47. | <p>Selling price = $300 + 200$ $= 500$ Marked price = $500 \div 0.8$ $= 625$ \therefore Marked price is \$625.</p> | <p>1 (47-1) 1* (47-2) 1** (47-3)</p> | Show the relation between selling price and marked price correctly | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 48. (9ME2-51) | <table border="1" style="width: 100%; text-align: center;"> <thead> <tr> <th colspan="2">Table 1</th> </tr> <tr> <th>Number of books borrowed</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>1 – 8</td> <td>4</td> </tr> <tr> <td>9 – 16</td> <td>5</td> </tr> <tr> <td>17 – 24</td> <td>4</td> </tr> <tr> <td>25 – 32</td> <td>3</td> </tr> <tr> <td>33 – 40</td> <td>2</td> </tr> <tr> <td>41 – 48</td> <td>2</td> </tr> </tbody> </table> <table border="1" style="width: 100%; text-align: center;"> <thead> <tr> <th colspan="2">Table 2</th> </tr> <tr> <th>Number of books borrowed</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>1 – 12</td> <td>6</td> </tr> <tr> <td>13 – 24</td> <td>7</td> </tr> <tr> <td>25 – 36</td> <td>5</td> </tr> <tr> <td>37 – 48</td> <td>2</td> </tr> </tbody> </table> | Table 1 | | Number of books borrowed | Frequency | 1 – 8 | 4 | 9 – 16 | 5 | 17 – 24 | 4 | 25 – 32 | 3 | 33 – 40 | 2 | 41 – 48 | 2 | Table 2 | | Number of books borrowed | Frequency | 1 – 12 | 6 | 13 – 24 | 7 | 25 – 36 | 5 | 37 – 48 | 2 | <p>1 (48-1) 1 (48-2)</p> | <p>Must be all correct Must be all correct</p> |
| Table 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Number of books borrowed | Frequency | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 – 8 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 9 – 16 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 17 – 24 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 – 32 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 33 – 40 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 41 – 48 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Table 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Number of books borrowed | Frequency | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 – 12 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 13 – 24 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 – 36 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 37 – 48 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 49. | <p>Range : 24 to 32</p> <p>The length of the living room is about the total length of 7 pieces of floor tiles. \therefore area $\approx 7 \times 4 \text{ m}^2 = 28 \text{ m}^2$.</p> | <p>1 (49-1) 1 (49-2)</p> | <p>Must have explanation The unit must be m^2 Other reasonable explanation (e.g. : In the figure, the width of the living room is about 4 m, the length is about 7 m, the area of the living room is about $4 \times 7 = 28 \text{ m}^2$.)</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 50. (a) | <p>Volume of the cone $= \frac{1}{3} \times 12^2 \times \pi \times 5$ $= 240 \pi \text{ cm}^3$</p> | <p>1 (50a-1) 1* (50a-2)</p> | <p>Correct set up</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (b) | <p>Curved surface area of the cone $= \pi \times 12 \times 13$ $= 156 \pi \text{ cm}^2$</p> | <p>1 (50b-1) 1* (50b-2) 1** (50-3)</p> | <p>Correct set up</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Question Number | Suggested Answers | | Marks | Notes |
|-----------------|--|-------------------------------|-------|--|
| 51. | $\angle ACB + \angle ACD = 180^\circ$ $\angle ACD = 26^\circ$ $\angle ACD = \angle CDE = 26^\circ$ $\therefore AC \parallel DE$ | adj. \angle s on a st. line | 3 | Any correct proof with correct reasons |
| | | alt \angle s equal | 2 | Any correct proof without reasons or having wrong symbol |
| | | | 1 | Incomplete proof with any one correct statement and one corresponding reason |
| | | | 0 | Incomplete proof |