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## Education Bureau

Territory-wide System Assessment 2013 Secondary 3
Mathematics

## QUESTION BOOKLET

## INSTRUCTIONS

1. There are 50 questions in this paper.
2. The time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
4. The use of HKEAA approved calculators is permitted.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

## FORMULAS FOR REFERENCE

| Sector | Arc length | $=2 \pi r \times \frac{\theta}{360^{\circ}}$ |
| :---: | :---: | :---: |
|  | Area | $=\pi r^{2} \times \frac{\theta}{360^{\circ}}$ |
| Sphere | Surface area | $=4 \pi r^{2}$ |
|  | Volume | $=\frac{4}{3} \pi r^{3}$ |
| Cylinder | Curved surfa | $=2 \pi r h$ |
|  | Volume | $=\pi r^{2} h$ |
| Cone | Curved surface area $=\pi r l$ |  |
|  | Volume | $=\frac{1}{3} \pi r^{2} h$ |
| Prism | Volume | $=$ base area $\times$ height |
| Pyramid | Volume | $=\frac{1}{3} \times \text { base area } \times \text { height }$ |

SECTION A: Choose the best answer for each question.
You should mark all your answers in the ANSWER BOOKLET.

1. In each of the following situations, determine whether the value mentioned is obtained by estimation or by computation of the exact value.
(i) It was reported on news that there were 400000 people watching the fireworks display on both sides of Victoria Harbour.
(ii) 132 photographs were displayed in an exhibition.
(i)
(ii)
A. Computation of the exact value Computation of the exact value
B. Computation of the exact value Estimation
C. Estimation

Computation of the exact value
D. Estimation

Estimation
2. Round off 0.048076 to 3 decimal places.
A. 0.05
B. 0.048
C. 0.0481
D. 0.04808
3. Alan bought 8 bottles of orange juice in a supermarket. He paid $\$ 100$ and the change was $\$ x$. Find the price of a bottle of orange juice.
A. $\$\left(\frac{100}{8}-x\right)$
B. $\$\left(\frac{100-x}{8}\right)$
C. $\$\left(\frac{100}{8}+x\right)$
D. $\$\left(\frac{100+x}{8}\right)$
4. The constant term of the polynomial $6 x^{3}+5 x^{2}+x+9$ is
A. 3.
B. 4 .
C. 6 .
D. 9 .
5. $(-4)^{3}=$
A. -64 .
B. -12 .
C. 12 .
D. 64 .
6. Ella bought $y$ model cars. Joseph bought 3 times as many model cars as Ella did. However, Joseph carelessly lost 2 cars. Now, he still has 16 cars left. Which of the following equations can be used to find the value of $y$ ?
A. $3 y-2=16$
B. $3 y+2=16$
C. $\frac{y}{3}-2=16$
D. $\frac{y}{3}+2=16$
7. Which of the following points lies on the straight line $y+2=0$ ?
A. $(-2,0)$
B. $(0,-2)$
C. $(2,0)$
D. $(0,2)$
8.


The above figure shows the graphs of $x-3 y-1=0$ and $20 x+21 y+42=0$.
Solve the simultaneous equations $\left\{\begin{array}{l}x-3 y-1=0 \\ 20 x+21 y+42=0\end{array}\right.$ graphically.
A. The approximate solution is $(-1.3,-0.8)$.
B. The exact solution is $(-1.3,-0.8)$.
C. The exact solution is $(-1.5,-1)$.
D. The approximate solution is $(-1.5,-1)$.
9. Which of the following diagrams represents $x \geq 8$ ?
A.

B.

C.

D.

10.


The figure shows a solid which is formed by a cube of side $a$ with a cylindrical portion being cut out. The radius and height of the removed cylindrical portion are $r$ and $a$ respectively. By considering the dimensions, determine which of the following could express the total surface area of the solid.
A. $12 a+4 \pi r$
B. $a\left(a^{2}-\pi r^{2}\right)$
C. $6 a^{2}+2 \pi r(a-r)$
D. $(a-r)\left(12 a-\pi r^{2}\right)$
11. In the figure, $A B C$ is a straight line. Which of the following is a straight angle?
A. $\angle A B C$
B. $\angle C B D$
C. $\angle D B E$
D. $\angle E B A$

12. The figure shows a right prism. Keith sketches a cross-section which is cut along the dotted line $P Q$ and is perpendicular to the base. Which of the following sketches is the plane diagram of the cross-section?

A.

B.

C.

D.

13.


Will the size and shape of the above figure be changed after translation?

|  | Size | Shape |
| :--- | :--- | :--- |
| A. | unchanged | unchanged |
| B. | unchanged | changed |
| C. | changed | unchanged |
| D. | changed | changed |

14. Which of the following figures shows that $x$ is an exterior angle of the quadrilateral?
A.

B.

C.

D.

15. Which of the following nets CANNOT be folded into a regular tetrahedron?

A.

B.

C.

D.

16. In the figure, $A B C D$ is a kite where $A B=A D$ and $B C=D C$.

Find the value of $x$.
A. $26^{\circ}$
B. $36^{\circ}$
C. $54^{\circ}$
D. $64^{\circ}$

17. In the figure, $\boldsymbol{P}(-3,4)$ is rotated about the origin $O$ through $270^{\circ}$ in a clockwise direction to $\boldsymbol{P}^{\prime}$. The coordinates of $\boldsymbol{P}^{\prime}$ are
A. $(4,3)$.
B. $(3,4)$.
C. $(-4,-3)$.
D. $(-3,-4)$.

18. Refer to the figure, find $\theta$. (Correct to the nearest degree)
A. $53^{\circ}$
B. $50^{\circ}$
C. $40^{\circ}$
D. $37^{\circ}$


26
19. Which of the following surveys is NOT suitable by using 'questionnaire' to collect the required data?
A. The survey about the further studies of S6 graduates of Perfect Secondary School
B. The survey about the number of credit cards owned by the students of Mathematics Department of Perfect University
C. The survey about the favourite fast food of P3 students of Perfect Primary School
D. The survey about the amount of sugar found in each type of bread sold at Perfect Bakery
20. The diagram below shows the volumes ( mL ) of 20 drinks.


If the above data is presented by a cumulative frequency polygon, which of the following should be obtained?
A.
Volumes of $\mathbf{2 0}$ drinks

C.

Volumes of $\mathbf{2 0}$ drinks

B.

Volumes of 20 drinks

D.

Volumes of 20 drinks


SECTION B: Write ALL the answers in the ANSWER BOOKLET. Working need not be shown.
21. Write down the numbers represented by $A, B$ and $C$ on the number line below.

22. The length of a bacterium is about 0.000003 m . Use scientific notation to represent this number.
23. During the 2012 Olympics in London, the numbers of medals won by Germany and the United States were in the ratio $11: 26$. If the United States won 104 medals, find the number of medals won by Germany.
24. In the figure, the total surface area $A$ of the solid cylinder can be calculated by the following formula:

$$
A=2 \pi r h+2 \pi r^{2}
$$

where $r$ and $h$ represent the base radius and the height of the solid cylinder respectively. If $r=3$ and $A=48 \pi$, find the value of $h$.

25. The $n^{\text {th }}$ term of a sequence is $\frac{n+6}{n+3}$. Find the value of the $7^{\text {th }}$ term of the sequence.
26. Expand $-2 x\left(x^{2}-3\right)$.
27. Factorize $a h+a k+3 h+3 k$.
28. Factorize $3 x^{2}+4 x+1$.
29.


The above figure shows the graph of $5 x-4 y-12=0$. Which of the following points lie(s) on the graph? (May be more than one answer)
$P(-3,0), \quad Q(0,-3), \quad R(3,1), \quad S(4,2)$
30. Consider the formula $S=\frac{a\left(r^{3}-1\right)}{r-1}$.

If $a=8$ and $r=3$, find the value of $S$.
31. According to the diagram, write down an inequality in $x$.

32. The length, width and height of a solid cuboid are $20 \mathrm{~cm}, 8 \mathrm{~cm}$ and 6 cm respectively. Find the total surface area of the cuboid.

33. Which of the following polygons is / are convex? (May be more than one answer)
P.

Q.

R.

S.

34. The figure below has rotational symmetry. Find its order of rotational symmetry.

35.


In the figure, $\triangle A B C \cong \triangle F G H$. Find the value of $k$.
36. In the figure, $\triangle A B C$ is an equilateral triangle. $B E D$ is a straight line, $\angle A B D=26^{\circ}$ and $A B=A D$. Find the value of $x$.

37. The figure shows a right prism $A B C D E F$. Its base $A B C$ is a triangle. Name the angle between the vertical plane $A B F E$ and the vertical plane $B C D F$.

38. Find the area of the figure $A B C D E F$ in the rectangular coordinate plane.

39. In the figure, $\tan \theta=\frac{8}{3}$. Find $\theta$. (Correct to the nearest $\left.0.1^{\circ}\right)$

40. In the figure, the slope of inclined road $B C$ is $\frac{3}{5}$. If the horizontal distance $A B$ is 45 m , find the vertical distance $A C$.

41. The following table shows the distribution of the lifespan of 50 AA batteries in a test.

| Lifespan (h) | $25-27$ | $28-30$ | $31-33$ | $34-36$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 8 | 14 | 22 | 6 |

Find the modal class of the lifespan of the 50 batteries.

SECTION C: All working must be clearly shown.
Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
42. In $\triangle A B C, \angle A B C=20^{\circ}$ and $\angle A C B=120^{\circ}$. Find $y$.

43. A wardrobe is sold for $\$ 2700$ at a loss of $25 \%$. Find the cost price of the wardrobe.
44. The figure shows a sphere of diameter 10 cm . Find the volume of the sphere. Correct the answer to the nearest $\mathrm{cm}^{3}$.

45. In the figure, the radius of sector $O A B$ is 24 cm and $\angle A O B=126^{\circ}$. Find the length of $\overparen{A B}$. Correct the answer to the nearest 0.1 cm .

46. The stem-and-leaf diagram below shows the marks obtained by 3B students in a Mathematics test.

Marks obtained by 3B students in a Mathematics test

| Stem (Tens digits) | Leaf (Units digits) |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | 5 | 6 | 6 | 7 | 8 | 9 |  |  |  |
|  | 4 | 1 | 2 | 3 | 6 | 8 | 8 |  |  |
|  | 5 | 2 | 3 | 4 | 4 | 7 | 7 | 8 | 8 |
| 6 | 0 | 2 | 7 | 9 |  |  |  |  |  |
| 7 | 3 | 6 | 9 |  |  |  |  |  |  |
| 8 | 2 | 3 | 7 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

According to the above diagram, answer the following questions.
(a) How many students are there in 3B?
(b) Find the median of the test marks.
(c) If the passing mark of this test is 50, find the percentage of students in 3B who pass the test.
47. Complete the table for the equation $y=2 x-1$ in the ANSWER BOOKLET.

| $x$ | -2 | 0 | 2 |
| :--- | :--- | :--- | :--- |
| $y$ |  |  | 3 |

According to the table, draw the graph of this equation on the rectangular coordinate plane given in the ANSWER BOOKLET.
48. In the figure, $A$ and $B$ are two circles. The circumference of $A$ is $8 \pi \mathrm{~cm}$. The circumference of $B$ is $6 \pi \mathrm{~cm}$ longer than that of $A$. Find the radius of $B$.


A


B
49. Solve the simultaneous equations $\left\{\begin{array}{l}3 x-y=20 \\ 2 x+y=15\end{array}\right.$.
50. Jacky went to a supermarket to buy 2 cans of baked beans with tomato sauce, 1 can of luncheon meat and 3 cans of corn soup. The prices of the items are listed below:

| Items | Baked beans with <br> tomato sauce | Luncheon meat | Corn soup |
| :---: | :---: | :---: | :---: |
| Unit price | $\$ 19.8$ | $\$ 14.7$ | $\$ 9.6$ |

Jacky found that he had $\$ 100$ only.
Based on the description above, give an approximation for the unit price of each item respectively. Use these 3 approximations to estimate the total amount required. Briefly explain whether Jacky had enough money to pay for the items.

## END OF PAPER

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