## $\mathbf{9} \mathbf{M E} \mathbf{1}$ ( $\mathbf{Q}$ )

## Education Bureau

Territory-wide System Assessment 2023

## Secondary 3 Mathematics QUESTION BOOKLET

## INSTRUCTIONS

1. There are 47 questions in this paper.
2. Time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
4. The use of HKEAA approved calculators is permitted.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

SECTION A: Choose the best answer for each question. You should mark all your answers in the ANSWER BOOKLET.

1. Find the greatest common divisor $(\mathrm{gcd})$ of $2^{2} \times 3$ and $2 \times 3^{2} \times 5$.
A. $2 \times 3$
B. $2 \times 3 \times 5$
C. $2^{2} \times 3^{2} \times 5$
D. $2^{3} \times 3^{3} \times 5$
2. Michael weighed 100 kg last year. His weight is 110 kg this year. Find the percentage change of his weight.
A. Decreased by $10 \%$
B. Decreased by $9.09 \%$
C. Increased by $9.09 \%$
D. Increased by $10 \%$
3. $x^{2}-y^{2}=$
A. $2 x-2 y$.
B. $x \cdot x-y \cdot y$.
C. $(x-y)^{2}$.
D. $x \cdot x+y \cdot y$.
4. There are 6 boxes of hand sanitiser. Each box contains $x$ bottles of hand sanitiser. If David buys 3 more bottles of hand sanitiser, all the bottles of hand sanitiser can be divided into 7 sets equally. How many bottles of hand sanitiser are there in each set?
A. $\left(\frac{6 x}{7}-3\right)$ bottles
B. $\left(\frac{6 x}{7}+3\right)$ bottles
C. $\frac{6 x-3}{7}$ bottles
D. $\frac{6 x+3}{7}$ bottles
5. Which of the following may represent the graph of the equation $x+y-7=0$ ?
A.

B.

C.

D.

6. 



The above figure shows the graphs of $2 x+3 y-18=0$ and $5 x-3 y-3=0$.
According to the given graphs, solve the simultaneous equations $\left\{\begin{array}{l}2 x+3 y-18=0 \\ 5 x-3 y-3=0\end{array}\right.$ graphically.
A. $(0,6)$
B. $(3,4)$
C. $(4,3)$
D. $(9,0)$
7. Nancy and Ivan weigh $x \mathrm{~kg}$ and $y \mathrm{~kg}$ respectively. Their total weight is 70 kg . 3 times Nancy's weight equals 2 times Ivan's weight. Which of the following pairs of simultaneous equations shows the relation between $x$ and $y$ ?
A. $\left\{\begin{array}{l}x+y=70 \\ 2 x=3 y\end{array}\right.$
B. $\left\{\begin{array}{l}x+y=70 \\ 3 x=2 y\end{array}\right.$
C. $\left\{\begin{array}{l}2 x+3 y=70 \\ 2 x=3 y\end{array}\right.$
D. $\left\{\begin{array}{l}3 x+2 y=70 \\ 3 x=2 y\end{array}\right.$
8. Which of the following polynomials is in descending powers of $x$ ?
A. $4 x+3-x^{2}$
B. $3+4 x-x^{2}$
C. $-x^{2}+3+4 x$
D. $-x^{2}+4 x+3$
9. $a(3 a+b-1)=$
A. $4 a+b-1$.
B. $4 a+a b-a$.
C. $3 a^{2}+a b-a$.
D. $3 a^{2}+b-1$.
10. Which of the following is an identity?
A. $x-3=3-x$
B. $2(x-3)=2 x-3$
C. $(x-3)(x+3)=x^{2}-9$
D. $(x+3)^{2}=x^{2}+9$
11. The figure shows a sticker $O A B$ with the shape of a sector. Its radius is 12 cm and $\angle A O B=150^{\circ}$. Find the area of the sticker.

A. $\pi(12) \times \frac{150^{\circ}}{360^{\circ}} \mathrm{cm}^{2}$
B. $2 \pi(12) \times \frac{150^{\circ}}{360^{\circ}} \mathrm{cm}^{2}$
C. $\pi(12)^{2} \times \frac{150^{\circ}}{360^{\circ}} \mathrm{cm}^{2}$
D. $2 \pi(12)^{2} \times \frac{150^{\circ}}{360^{\circ}} \mathrm{cm}^{2}$
12. A regular tetrahedron is placed horizontally as shown. Raymond sketches a section which is perpendicular to the base and passing through vertex $A$.


Which of the following can be the plane diagram of the section?
A.

B.

C.

D.

13. The figure shows a solid right circular cylinder. Its curved surface area is $500 \pi \mathrm{~cm}^{2}$. Its base radius is 10 cm . Find the height of the cylinder.

A. 5 cm
B. 15 cm
C. 25 cm
D. 50 cm
14. In the figure, $A B / / C D$ and $E F$ is a straight line. Which of the following are a pair of corresponding angles?
A. $\quad a$ and $b$
B. $\quad a$ and $d$
C. $c$ and $b$
D. $c$ and $d$

15. Which of the following pairs of triangles MUST be congruent?
A.

5

B.

C.


D.

16. In the figure, $A B C D$ is a parallelogram. $A C$ and $B D$ intersect at point $E . A E=7 \mathrm{~cm}$, $B E=9 \mathrm{~cm}$ and $D E=y \mathrm{~cm}$. Find the value of $y$.

A. 2
B. 7
C. 9
D. 16
17. In $\triangle A B C, B D C$ is a straight line. If $\angle B A D=\angle D A C, A D$ MUST be
A. an angle bisector of $\triangle A B C$.
B. a median of $\triangle A B C$.
C. an altitude of $\triangle A B C$.
D. a perpendicular bisector of $\triangle A B C$.

18. $P(9,0)$ and $Q(-3,2)$ are two points on a straight line $L$ in the rectangular coordinate plane. The slope of $L=$
A. $\frac{2-0}{-3-9}$.
B. $\frac{-3-9}{2-0}$.
C. $\frac{2+0}{-3+9}$.
D. $\frac{-3+9}{2+0}$.
19. The table below shows the water consumption $\left(\mathrm{m}^{3}\right)$ of a restaurant last week.

| Day of <br> the Week | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Water <br> Consumption $\left(\mathrm{m}^{3}\right)$ | 30.0 | 30.1 | 28.1 | 31.2 | 34.8 | 39.6 | 42.0 |

Which of the following is the most suitable for presenting the data above?
A. Pie chart
B. Broken line graph
C. Stem-and-leaf diagram
D. Histogram
20. Carmen applied for admission to a secondary school. The table below shows the weights of the admission criterion and her marks in these areas.

|  | Admission Criterion |  |  |
| :---: | :---: | :---: | :---: |
|  | Interview | Learning <br> Portfolio | Extra-Curricular <br> Activity |
| Mark | 70 | 80 | 90 |
| Weight | 5 | 3 | 2 |

Find the weighted mean mark of Carmen.
A. 24
B. 77
C. 80
D. 240

SECTION B: Write ALL the answers in the ANSWER BOOKLET. Working need not be shown.
21. Express 45 as a product of prime factors.
22. Brian used directed numbers to represent the time differences between Hong Kong and other regions.
For example,
-5 hours represents that the local time in region $A$ is 5 hours behind the local time in Hong Kong.
Use a directed number to represent each of the following situations.
(i) The local time in Seoul is 1 hour ahead of the local time in Hong Kong.
(ii) The local time in New York is 12 hours behind the local time in Hong Kong.
23. If $\sqrt[3]{a}=8$, find the value of $a$.
24. Solve the equation $2(x-3)-7=8-5 x$.
25. In each of the following situations, determine whether the relationship between $x$ and $y$ is direct proportion or inverse proportion.
(i) The selling price of an apple is $\$ 3$. Mary pays $\$ y$ to buy $x$ apples.
(ii) A teacher shares 30 candies between $x$ students equally. Each student gets $y$ candies.
26. Factorise $x^{2}+12 x+36$.
27. Expand $(x-1)(x+5)$.
28. Factorise $x^{2}-7 x+6$.
29. Simplify $\frac{1}{2 x}+\frac{2}{x}$.
30. According to the diagram, write down an inequality in $x$.

31. The figure shows the diagram of a right pyramid:


Referring to the sketch shown above, add 1 solid line and 1 dotted line in the figure provided in the ANSWER BOOKLET so as to form a diagram of a right hexagonal prism.
32. In the figure, $A G B$ and $G D F$ are straight lines. $A B, C D$ and $E F$ are parallel lines. It is given that $\angle C D F=115^{\circ}$. Find $x$.

33. In the figure, $A E C$ and $D E B$ are straight lines. $\triangle E A B$ and $\triangle D E C$ are isosceles triangles, where $E A=E B$ and $D C=D E$. It is given that $\angle C D E=40^{\circ}$. Find $x$.

34. In the figure, $\triangle A B C \cong \triangle P Q R$. Find
(a) the value of $x$,
(b) the value of $y$.

35.


Which of the following triangles MUST be similar to $\triangle A B C$ as shown in the above figure? (May be more than one answer)

Triangle $P$


Triangle $Q$

36. Find the value of $x$ in the figure. (Correct to 3 significant figures)

37. The histogram below shows the average daily amount of browsing time on the Internet of Secondary 3 students in a school.

Average daily amount of browsing time on the Internet of Secondary 3 students


According to the above histogram, answer the following questions.
(a) Complete the frequency distribution table in the ANSWER BOOKLET.
(b) Find the total number of Secondary 3 students in the school.
(c) If a student's average daily amount of browsing time on the Internet is 60.5 minutes or more, he/she has to join an activity called "Master of Time Management". Find the number of Secondary 3 students joining the activity.
38. The following data shows the number of homework submitted late by Jason in the last 8 months.

$$
13, \quad 3, \quad 5,9,12,12,13,13
$$

Find the mean and the median of the above data.
39. Wilson throws a dice 100 times. The outcomes are shown as follows:

| Outcome | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 12 | 20 | 14 | 28 | 14 | 12 |

Find the relative frequency of Wilson getting an even number.

SECTION C: All working must be clearly shown.
Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
40. Paul deposits $\$ 5720$ in a bank at a simple interest rate of $3 \%$ p.a. Find the interest he will receive after 5 years.
41. In a city, 2000 people got influenza three months ago. If the number of infected people is decreasing by $30 \%$ monthly, find the number of people getting influenza in the city this month.
42. Complete the table for the equation $y=2 x+1$ in the ANSWER BOOKLET.

| $x$ | -3 | 0 | 2 |
| :--- | :--- | :--- | :--- |
| $y$ |  | 1 |  |

According to the table, plot the graph of this equation on the rectangular coordinate plane given in the ANSWER BOOKLET.
43. (a) Simplify $x^{-4} \cdot x^{6}$ and express the answer with positive index.
(b) Simplify $\left(x^{-4} \cdot x^{6}\right)^{5}$ and express the answer with positive index.
44. In the figure, $B D F$ and $C E D$ are straight lines. It is given that $\angle A B D=30^{\circ}$, $\angle D E F=86^{\circ}$ and $\angle E F D=64^{\circ}$. Prove that $A B / / C D$.

45. In the figure, $A B C D$ is a rhombus. $A C$ and $B D$ are perpendicular to each other and they intersect at point $E$. It is given that $A E=7 \mathrm{~cm}$ and $B E=2.4 \mathrm{~cm}$. Find the perimeter of the rhombus.

46. Find the area of $\triangle A B C$ in the figure.

47. The prices of drinks at a restaurant are shown as follows:

| Drink | Price |
| :---: | :---: |
| Green Tea | $\$ 14$ |
| Red Tea | $\$ 14$ |
| Lemon Water | $\$ 16$ |
| Lemon Tea | $\$ 16$ |
| Coffee | $\$ 17$ |
| Milk Tea | $\$ 17$ |
| Chocolate Milk | $\$ 24$ |
| Fresh Milk | $\$ 26$ |

A customer said, 'Since the mean price of all types of drinks is $\$ 18$, over half of the types of drinks are $\$ 18$ or more.'

Do you agree with the customer's claim? Explain your answer.

## END OF PAPER

## Do not write on this page.

Answers written on this page will not be marked.
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Prepared by the Hong Kong Examinations and Assessment Authority

## 9 M E 1 ( $\mathbf{A}$ )

# Education Bureau <br> Territory-wide System Assessment 2023 

## Secondary 3 Mathematics ANSWER BOOKLET

## INSTRUCTIONS

1. Write your School Code, Class and Class Number in the boxes provided on this page.
2. Stick barcode labels in the spaces provided on page 1 and page 3 .
3. Time allowed is 65 minutes.
4. Write ALL your answers in the spaces provided in this ANSWER BOOKLET.
5. Do not write in the margins.
6. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
7. The use of HKEAA approved calculators is permitted.
8. Rough work should be done on the rough work sheet provided.


## SECTION A: Multiple Choice Questions

| MC Questions - Blacken the circle under the correct answer |
| :---: |
| with an HB pencil. For example : |
| A |

1. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
2. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
3. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
4. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
5. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
6. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
7. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C} \quad \mathrm{D}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
8. A B C D
$\bigcirc \bigcirc \bigcirc$
9. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C} D$
$\bigcirc \bigcirc \bigcirc$
10. A B C D
$\bigcirc \bigcirc \bigcirc$

Please stick the barcode label in the box. $\longrightarrow$
Please do not write in the margin.
11. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
12. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
13. A B C D
$\bigcirc \bigcirc \bigcirc$
14. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
15. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
16. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
17. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
18. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
19. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
20. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$

## SECTION B: Write your answers in the spaces provided. Working need not

 be shown.21. $\qquad$
22. (i) $\qquad$ hour(s) represents that the local time in Seoul is 1 hour ahead of the local time in Hong Kong.
(ii) $\qquad$ hour(s) represents that the local time in New York is 12 hours behind the local time in Hong Kong.
23. 

$a=$ $\qquad$
24.
$x=$ $\qquad$
25. *Circle the correct answer
(i) * Direct proportion / Inverse proportion
(ii) * Direct proportion / Inverse proportion
26. $\qquad$
27. $\qquad$
28. $\qquad$
29. $\qquad$
30. $\qquad$
31. Diagram of a right hexagonal prism:

32. $x=$ $\qquad$
33. $x=$ $\qquad$
34. (a) $x=$ $\qquad$
(b) $y=$ $\qquad$
35. $\qquad$
36. $x=$ $\qquad$
37. (a)

| Time (minutes) | $31-40$ | $41-50$ | $51-60$ | $61-70$ | $71-80$ | $81-90$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 |  | 17 |  | 21 |  |

(b) The total number of Secondary 3 students in the school is $\qquad$ .
(c) The number of Secondary 3 students joining the activity is $\qquad$ .
38. Mean = $\qquad$
Median = $\qquad$
39. The required relative frequency $=$ $\qquad$

## SECTION C: Answer in the spaces provided.

 All working and conclusions must be clearly shown.40. $\qquad$
41. $\qquad$
42. 

| $y=2 x+1$ |
| :---: | :---: | :---: | :---: |
| $x$ -3 0 <br> 2   <br> $y$  1 |


Please do not write in the margin.
43.

46. $\qquad$
47. Reason:
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\therefore$ I * agree / disagree with the customer's claim. (*Circle the correct answer)
END OF PAPER

## $\mathbf{9} \mathbf{M E} \mathbf{2}(\mathbf{Q})$

## Education Bureau

Territory-wide System Assessment 2023

## Secondary 3 Mathematics QUESTION BOOKLET

## INSTRUCTIONS

1. There are 47 questions in this paper.
2. Time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
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5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

SECTION A: Choose the best answer for each question. You should mark all your answers in the ANSWER BOOKLET.

1. Round off 0.06987 to 3 decimal places.
A. 0.069
B. 0.0699
C. 0.07
D. 0.070
2. Which of the following is an irrational number?
A. 0.14
B. $\sqrt[3]{27}$
C. $2 \pi$
D. $\frac{1}{3}$
3. Which of the following statements is correct?
A. The solution of $x-8=0$ is $-\frac{1}{8}$.
B. The solution of $x+8=0$ is $-\frac{1}{8}$.
C. The solution of $8 x-1=0$ is $-\frac{1}{8}$.
D. The solution of $8 x+1=0$ is $-\frac{1}{8}$.
4. 



The above figure shows the graphs of $2 x+3 y-18=0$ and $5 x-3 y-3=0$.
According to the given graphs, solve the simultaneous equations $\left\{\begin{array}{l}2 x+3 y-18=0 \\ 5 x-3 y-3=0\end{array}\right.$ graphically.
A. $(0,6)$
B. $(3,4)$
C. $(4,3)$
D. $(9,0)$
5. $(-4)^{-3}=$
A. -64 .
B. 64 .
C. $-\frac{1}{64}$.
D. $\frac{1}{64}$.
6. $1.86 \times 10^{3}=$
A. 1860 .
B. 186000 .
C. 0.00186 .
D. 0.000186 .
7. Which of the following polynomials is in descending powers of $x$ ?
A. $4 x+3-x^{2}$
B. $3+4 x-x^{2}$
C. $-x^{2}+3+4 x$
D. $-x^{2}+4 x+3$
8. Determine whether each of the following is factorisation or expansion.
(i) $\begin{aligned} & (2 x-1)(x-1)(x-3) \\ = & 2 x^{3}-9 x^{2}+10 x-3\end{aligned}$
(ii) $\begin{gathered}2 x^{3}-9 x^{2}+10 x-3 \\ =(2 x-1)(x-1)(x-3)\end{gathered}$
A. (i) Factorisation
(ii) Factorisation
B. (i) Expansion
(ii) Factorisation
C. (i) Factorisation
(ii) Expansion
D. (i) Expansion
(ii) Expansion
9. If $x \geq-3$, which of the following CANNOT be the value of $x$ ?
A. 0
B. -2
C. -3
D. -4
10. A shop sells two kinds of candies including lollipops and chocolate. One pack of lollipops weighs $x \mathrm{~g}$. The weight of a pack of chocolate is half that of a pack of lollipops. Susan has 3 packs of lollipops and 4 packs of chocolate. The total weight of the candies does not exceed 750 g . Which of the following inequalities can be used to find the range of the values of $x$ ?
A. $3 x+4 \times\left(\frac{x}{2}\right)>750$
B. $3 x+4 \times\left(\frac{x}{2}\right)<750$
C. $3 x+4 \times\left(\frac{x}{2}\right) \geq 750$
D. $3 x+4 \times\left(\frac{x}{2}\right) \leq 750$
11. The thickness of a glass is 6 mm (correct to the nearest mm ). Which of the following could be its actual thickness?
A. 5.3 mm
B. $\quad 5.4 \mathrm{~mm}$
C. $\quad 6.4 \mathrm{~mm}$
D. 6.5 mm
12. A regular tetrahedron is placed horizontally as shown. Raymond sketches a section which is perpendicular to the base and passing through vertex $A$.


Which of the following can be the plane diagram of the section?
A.

B.

C.

D.

13. The figure shows a solid right circular cylinder. Its curved surface area is $500 \pi \mathrm{~cm}^{2}$. Its base radius is 10 cm . Find the height of the cylinder.

A. 5 cm
B. 15 cm
C. 25 cm
D. 50 cm
14. In the figure, $A B / / C D$ and $E F$ is a straight line. Which of the following are a pair of corresponding angles?
A. $\quad a$ and $b$
B. $\quad a$ and $d$
C. $c$ and $b$
D. $c$ and $d$

15. Which of the following pairs of triangles MUST be similar?
A.

B.


C.

D.

16. In $\triangle A B C, B D C$ is a straight line. If $\angle B A D=\angle D A C, A D$ MUST be
A. an angle bisector of $\triangle A B C$.
B. a median of $\triangle A B C$.
C. an altitude of $\triangle A B C$.
D. a perpendicular bisector of $\triangle A B C$.

17. In the figure, $\boldsymbol{R}(0,3)$ is rotated about the origin $O$ through $90^{\circ}$ in a clockwise direction to $\boldsymbol{R}^{\prime}$. Find the coordinates of $\boldsymbol{R}^{\prime}$.
A. $(0,-3)$
B. $(-3,0)$
C. $(3,0)$
D. $(0,3)$

18. Referring to the figure, find $\theta$. (Correct to 3 significant figures)
A. $34.8^{\circ}$
B. $44.1^{\circ}$
C. $45.9^{\circ}$
D. $55.2^{\circ}$

19. The table below shows the water consumption $\left(\mathrm{m}^{3}\right)$ of a restaurant last week.

| Day of <br> the Week | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Water <br> Consumption $\left(\mathrm{m}^{3}\right)$ | 30.0 | 30.1 | 28.1 | 31.2 | 34.8 | 39.6 | 42.0 |

Which of the following is the most suitable for presenting the data above?
A. Pie chart
B. Broken line graph
C. Stem-and-leaf diagram
D. Histogram
20. The diagram below shows the attendance at two theme parks in a day.


Based on the diagram above, Charles believes that the attendance at "Ocean World" is double the attendance at "Joyful Park" on that day.
Which of the following statements is the best reason that Charles is misled by the above diagram?
A. The scale of vertical axis in the diagram does not start from 0
B. The number of days the two theme parks were open is not shown.
C. The attendance on other days is not shown.
D. The number of staff at the two theme parks is not shown.

SECTION B: Write ALL the answers in the ANSWER BOOKLET. Working need not be shown.
21. Calculate $6 \times[4+(7-10 \div 2)]$.
22. Calculate $\frac{(-5)(-3)}{-2-3}$.
23. Calculate $\sqrt[3]{1728}$.
24. The electricity consumption of a company was 1140 kWh last month. It decreased by $15 \%$ this month. Find the electricity consumption of the company this month.
25. Find the value of $x$ in the following sequence of triangular numbers.

$$
1,3,6,10,15,21,28, x, \ldots
$$

26. Solve the equation $2(x-3)-7=8-5 x$.
27. Find the coefficient of $x^{2}$ in the polynomial of $5 x^{3}-7 x^{2}+6 x-9$.
28. Factorise $5(x+y)-a(x+y)$.
29. Expand $(y-4)^{2}$.
30. Simplify $\left(\frac{x^{2}}{8 y}\right)\left(\frac{16 y}{x}\right)$.
31. Make $y$ the subject of the formula $w=k+\frac{y}{5}$.
32. In each of the following solids, their bases $B C D E$ are squares. Which of the following MUST be a right pyramid?

Solid $P$
Solid $Q$
Solid $R$

33. In the figure, the base of the prism is a right-angled triangle. The base and the height of the right-angled triangle are 12 cm and 5 cm respectively. The height of the prism is 18 cm . Find the volume of the prism.

34. In the figure, $B D C$ is a straight line. $\triangle A B C$ is an isosceles triangle, where $A B=A C$. It is given that $\angle A C D=35^{\circ}$ and $\angle B A D=20^{\circ}$. Find $x$.

35. In the figure, $A C$ is the diagonal of rectangle $A B C D$. It is given that $\angle B A C=50^{\circ}$. Find $x$.

36. In the figure, $P$ is a point on the horizontal ground. Find the angle of elevation of $Q$ from $P$.

37. The histogram below shows the average daily amount of browsing time on the Internet of Secondary 3 students in a school.


According to the above histogram, answer the following questions.
(a) Complete the frequency distribution table in the ANSWER BOOKLET.
(b) Find the total number of Secondary 3 students in the school.
(c) If a student's average daily amount of browsing time on the Internet is 60.5 minutes or more, he/she has to join an activity called "Master of Time Management". Find the number of Secondary 3 students joining the activity.
38. The diagram below shows the average relative humidity from January to June in 2021 and 2022.

Average relative humidity from January to June in 2021 and 2022


According to the above diagram, in which month is the average relative humidity the same in 2021 and 2022 ?
39. The following data shows the number of homework submitted late by Jason in the last 8 months.

$$
13, \quad 3, \quad 5, \quad 9, \quad 12, \quad 12, \quad 13, \quad 13
$$

Find the mean and the median of the above data.

SECTION C: All working must be clearly shown.
Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
40. It is recommended that the standard daily calorie intake of a male adult should not exceed 2500 calories. Mr Chan ate instant noodles, pizza and roast goose today. The calories are 381, 532 and 1706 respectively.

Based on the description above, give an appropriate approximation for each UNDERLINED VALUE. Hence, estimate the total calorie intake of Mr Chan today. Briefly explain whether his calorie intake today is over the standard.
41. There is a box of facemasks. If it is distributed to 4 persons, each person can get 15 facemasks. If this box of facemasks is distributed to 6 persons equally, how many facemasks can each person get?
42. Solve the simultaneous equations $\left\{\begin{array}{l}y=3 x+8 \\ x+y=4\end{array}\right.$.
43. In the figure, the radius of sector $O A B$ is 4 cm and $\angle A O B=95^{\circ}$. Let $x$ be the arc length of the sector, find $x$. Give the answer correct to 3 significant figures.

44. In the figure, Ball $A$ and Ball $B$ are similar solids. The diameter of Ball $A$ is 3 times that of Ball $B$. The volume of Ball $A$ is $2700 \mathrm{~cm}^{3}$. Find the volume of Ball $B$.


Ball $A$


Ball B
45. In the figure, $\angle A B C=50^{\circ}$ and $\angle C A B=65^{\circ}$. Prove that $\triangle B C A$ is an isosceles triangle.

46. The figure shows a map of an orienteering competition. It is given that the distance of $A B$ is 5 km and the distance of $B C$ is 3 km .
Find $\angle A C B$. Give the answer correct to 3 significant figures.

47. The following data shows the number of absentees of a secondary school in the last 15 school days.

| 9 | 12 | 17 | 18 | 20 |
| :---: | :---: | :---: | :---: | :---: |
| 15 | 8 | 25 | 14 | 30 |
| 42 | 36 | 7 | 22 | 15 |

Complete the stem-and-leaf diagram in the ANSWER BOOKLET to represent the above data.

## END OF PAPER

## Do not write on this page.

Answers written on this page will not be marked.
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## $\left.\begin{array}{l|l|l|l|l|l}\mathbf{9} & \mathbf{M} & \mathbf{E} & \mathbf{2} & ( & \mathbf{A}\end{array}\right)$

# Education Bureau <br> Territory-wide System Assessment 2023 

## Secondary 3 Mathematics ANSWER BOOKLET

## INSTRUCTIONS

1. Write your School Code, Class and Class Number in the boxes provided on this page.
2. Stick barcode labels in the spaces provided on page 1 and page 3 .
3. Time allowed is 65 minutes.
4. Write ALL your answers in the spaces provided in this ANSWER BOOKLET.
5. Do not write in the margins.
6. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
7. The use of HKEAA approved calculators is permitted.
8. Rough work should be done on the rough work sheet provided.


## SECTION A: Multiple Choice Questions

| MC Questions - Blacken the circle under the correct answer |
| :---: |
| with an HB pencil. For example : |
| A |
| A |

1. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
2. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
3. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
4. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
5. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
6. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
7. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
8. A B C D
$\bigcirc \bigcirc \bigcirc$
9. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C} D$
$\bigcirc \bigcirc \bigcirc$
10. A B C D
$\bigcirc \bigcirc \bigcirc$

Please stick the barcode label in the box. $\longrightarrow$
Please do not write in the margin.
11. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
12. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
13. A B C D
$\bigcirc \bigcirc \bigcirc$
14. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
15. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
16. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
17. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
18. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
19. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
20. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$

SECTION B: Write your answers in the spaces provided. Working need not be shown.
21. $\qquad$
22. $\qquad$
23. $\qquad$
24. The electricity consumption of the company is $\qquad$ this month.
25. $x=$ $\qquad$
26. $x=$ $\qquad$
27. The coefficient of $x^{2}$ is $\qquad$ .
28. $\qquad$
29. $\qquad$
30. $\qquad$
31. $\qquad$
32. $\qquad$
33. The volume of the prism is $\qquad$ .
34. $x=$ $\qquad$
35. $x=$ $\qquad$
36. The angle of elevation of $Q$ from $P$ is $\qquad$ .
37. (a)

| Time (minutes) | $31-40$ | $41-50$ | $51-60$ | $61-70$ | $71-80$ | $81-90$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 |  | 17 |  | 21 |  |

(b) The total number of Secondary 3 students in the school is $\qquad$ .
(c) The number of Secondary 3 students joining the activity is $\qquad$ .
38. In 2021 and 2022, the average relative humidity in $\qquad$ is the same.
39. Mean = $\qquad$
Median $=$ $\qquad$
SECTION C: Answer in the spaces provided. All working and conclusions must be clearly shown.
40.

41. $\qquad$
42. $\qquad$
43.



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## $\mathbf{9} \mathbf{M E} \mathbf{3}(\mathbf{Q})$

## Education Bureau

Territory-wide System Assessment 2023

## Secondary 3 Mathematics QUESTION BOOKLET

## INSTRUCTIONS

1. There are 47 questions in this paper.
2. Time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
4. The use of HKEAA approved calculators is permitted.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

SECTION A: Choose the best answer for each question. You should mark all your answers in the ANSWER BOOKLET.

1. $2^{3}=$
A. $2 \times 3$.
B. $2 \times 2 \times 2$.
C. $3 \times 3$.
D. $2+3$.
2. Which of the following is an irrational number?
A. 0.14
B. $\sqrt[3]{27}$
C. $2 \pi$
D. $\frac{1}{3}$
3. Mary used cocoa powder and sugar in the ratio $2: 5$ by weight to make chocolate cupcakes. What is the weight of the cocoa powder needed if she used 140 g of sugar to make chocolate cupcakes?
A. 40 g
B. 56 g
C. $\quad 100 \mathrm{~g}$
D. 350 g
4. Which of the following statements is correct?
A. The solution of $x-8=0$ is $-\frac{1}{8}$.
B. The solution of $x+8=0$ is $-\frac{1}{8}$.
C. The solution of $8 x-1=0$ is $-\frac{1}{8}$.
D. The solution of $8 x+1=0$ is $-\frac{1}{8}$.
5. Jack took $x$ seconds to complete 26 multiple choice questions. If he spends 1 second less on average for each multiple choice question, he will complete 2 more multiple choice questions in the same amount of time. Which of the following equations can be used to find the value of $x$ ?
A. $\frac{x}{26}-1=2$
B. $\frac{x}{24}-\frac{x}{26}=1$
C. $\frac{x}{26}-\frac{x}{28}=1$
D. $\frac{x}{2}-\frac{x}{26}=1$
6. Which of the following points lies on the straight line $y=9 x+3$ ?
A. $(0,3)$
B. $(3,0)$
C. $(-1,6)$
D. $(1,-6)$
7. Simplify $\frac{x^{2}}{2 x^{-3}}$.
A. $\frac{x}{2}$
B. $2 x$
C. $2 x^{5}$
D. $\frac{x^{5}}{2}$
8. $1.86 \times 10^{3}=$
A. 1860 .
B. 186000 .
C. 0.00186 .
D. 0.000186 .
9. Which of the following is NOT a polynomial?
A. $3+\frac{2}{y^{2}}$
B. $3+\frac{y^{2}}{2}$
C. $3+2 y$
D. $3+2 y^{2}$
10. If $x \leq y$, which of the following inequalities is correct?
A. $\frac{x}{3} \geq \frac{y}{3}$
B. $3 x \geq 3 y$
C. $-3 x \leq-3 y$
D. $x-3 \leq y-3$
11. Jack uses a protractor to measure an angle and the result is $50^{\circ}$ (correct to the nearest $1^{\circ}$ ). Find the maximum absolute error of the measurement.
A. $0.1^{\circ}$
B. $0.5^{\circ}$
C. $1^{\circ}$
D. $5^{\circ}$

12. The figure shows a sphere. Its radius is 9 cm . Find the volume of the sphere.

A. $2 \pi(9)^{2} \mathrm{~cm}^{3}$
B. $4 \pi(9)^{2} \mathrm{~cm}^{3}$
C. $\frac{1}{3} \pi(9)^{3} \mathrm{~cm}^{3}$
D. $\frac{4}{3} \pi(9)^{3} \mathrm{~cm}^{3}$
13. In each of the following figures, $P Q$ is a straight line. Which figure shows that $x$ and $y$ are a pair of alternate interior angles?
A.

B.

C.

D.

14. Which of the following represents the rhombus in the figure?
A. $P Q R S$
B. $\triangle P Q R$
C. $P R$
D. $P$

15. Which of the following pairs of triangles MUST be similar?
A.

B.

C.

D.

16. In the figure, $\triangle P Q R$ is a right-angled triangle. If $P Q=55$ and $Q R=48$, find $P R$.
A. $\sqrt{55+48}$
B. $\sqrt{55^{2}-48^{2}}$
C. $\sqrt{55^{2}+48^{2}}$
D. $55^{2}+48^{2}$

17. In the figure, $\boldsymbol{R}(0,3)$ is rotated about the origin $O$ through $90^{\circ}$ in a clockwise direction to $\boldsymbol{R}^{\prime}$. Find the coordinates of $\boldsymbol{R}^{\prime}$.
A. $(0,-3)$
B. $(-3,0)$
C. $(3,0)$
D. $(0,3)$

18. It is given that the slope of a straight line $\ell$ is $-\frac{1}{6}$. Which of the following straight lines is parallel to $\ell$ ?

| Line | $L_{1}$ | $L_{2}$ | $L_{3}$ | $L_{4}$ |
| :---: | :---: | :---: | :---: | :---: |
| Slope | 6 | -6 | $\frac{1}{6}$ | $-\frac{1}{6}$ |

A. $L_{1}$
B. $L_{2}$
C. $L_{3}$
D. $L_{4}$
19. The diagram below shows the attendance at two theme parks in a day.


Based on the diagram above, Charles believes that the attendance at "Ocean World" is double the attendance at "Joyful Park" on that day.
Which of the following statements is the best reason that Charles is misled by the above diagram?
A. The scale of vertical axis in the diagram does not start from 0 .
B. The number of days the two theme parks were open is not shown.
C. The attendance on other days is not shown.
D. The number of staff at the two theme parks is not shown.
20. The following table shows the service status of trains and their corresponding frequency at a station yesterday.

| Service status | Left ahead of time | Left on time | Left behind schedule |
| :---: | :---: | :---: | :---: |
| Frequency | 0 | 1997 | 3 |

Find the relative frequency of the service status "left behind schedule" at the station yesterday.
A. 0
B. $\frac{1997}{2000}$
C. $\frac{3}{2000}$
D. $\frac{3}{1997}$

SECTION B: Write ALL the answers in the ANSWER BOOKLET. Working need not be shown.
21. Calculate $6 \times[4+(7-10 \div 2)]$.
22. Calculate $\frac{(-5)(-3)}{-2-3}$.
23. Use the symbol ' $x$ ' to mark the number -0.25 on the number line given in the ANSWER BOOKLET.

Example : 1.5 is marked on the number line below.

24. The marked price of a cake is $\$ 320$. If it is sold at $30 \%$ off, find the discount.
25. The $n$th term of a sequence is $4+2(n-1)$. Find the value of the 3 rd term of the sequence.
26. Find the value of $(-5)^{0}$.
27. Expand $(y-4)^{2}$.
28. Factorise $25 x^{2}-1$.
29. Consider the formula $c=\frac{a b}{a+b}$. If $a=10$ and $b=15$, find the value of $c$.
30. Solve the inequality $4 x+7<-1$.
31. In the figure, $A O B$ and $C O D$ are straight lines. $\angle C O E=35^{\circ}$ and $\angle B O D=120^{\circ}$. Find $x$.

32. The figure shows a hexagon $A B C D E F$. Find $x$.

33. In the figure, $A C$ is the diagonal of rectangle $A B C D$. It is given that $\angle B A C=50^{\circ}$. Find $x$.

34. Which of the following MUST be right-angled triangle(s)? (May be more than one answer)

Triangle $R$

35. Find the distance between two points $P(9,13)$ and $Q(3,5)$ in the rectangular coordinate plane.
36. In the figure, $\sin x^{\circ}=\frac{1}{\sqrt{7}}$. Find the value of $x$. (Correct to 3 significant figures)

37. The following data shows the average traffic flow (number of vehicles per minute) of a location in last 15 days.

| 42 | 20 | 5 | 30 | 12 |
| :---: | :---: | :---: | :---: | :---: |
| 44 | 40 | 36 | 22 | 24 |
| 33 | 38 | 16 | 18 | 24 |

Use the data to complete the two frequency distribution tables in the ANSWER BOOKLET.
38. The cumulative frequency curve below shows the result of the lifetime of some batteries in a test.

Test result of the lifetime of batteries


According to the cumulative frequency curve shown above, answer the following questions.
(a) How many batteries have been examined in the test?
(b) Find the median of the lifetime of batteries in the test.
(c) If the lifetime of a battery is not more than 2 hours, its quality does not meet the requirement. How many batteries do not meet the requirement in the test?
39. Simon joined an admission examination for a university this year. The following table shows the weight in each subject of the admission scoring scheme and his scores in these subjects.

|  | Subject |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | English Language | Mathematics | Chemistry | Physics |
| Score | 4 | 5 | 2 | 3 |
| Weight | $40 \%$ | $30 \%$ | $10 \%$ | $20 \%$ |

Find the weighted mean score of Simon.

SECTION C: All working must be clearly shown.
Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
40. Winnie deposits $\$ 5000$ in a bank and the interest rate is $8 \%$ p.a. compounded yearly. Find the interest she will receive after 2 years.
41. Complete the table for the equation $2 x-y+1=0$ in the ANSWER BOOKLET.

| $x$ | -3 | 0 | 2 |
| :--- | :--- | :--- | :--- |
| $y$ |  | 1 |  |

According to the table, plot the graph of this equation on the rectangular coordinate plane given in the ANSWER BOOKLET.
42. Solve the simultaneous equations $\left\{\begin{array}{l}y=3 x+8 \\ x+y=4\end{array}\right.$.
43. In the figure, the radius of sector $O A B$ is 4 cm and $\angle A O B=95^{\circ}$. Let $x$ be the arc length of the sector, find $x$. Give the answer correct to 3 significant figures.

44. In the figure, the volume of a solid triangular prism is $768 \mathrm{~cm}^{3}$. Its base area is $64 \mathrm{~cm}^{2}$. The height of the prism is $h \mathrm{~cm}$. Find the value of $h$.

45. In the figure, $A C D$ is a straight line. $\angle B A D=45^{\circ}$ and $\angle B C D=3 x-75^{\circ}$. Find $x$.

46. In the figure, $A C E$ and $B C D$ are straight lines. $C B=3 \mathrm{~cm}, C A=5 \mathrm{~cm}, C D=9 \mathrm{~cm}$ and $C E=15 \mathrm{~cm}$. Prove that $\triangle C A B \sim \triangle C E D$.

47. The following table shows the distribution of the weight of 24 tomatoes.

| Weight $(\mathrm{g})$ | Class Mark $(\mathrm{g})$ | Frequency |
| :---: | :---: | :---: |
| $150-169$ | 159.5 | 7 |
| $170-189$ | 179.5 | 6 |
| $190-209$ | 199.5 |  |
| $210-229$ | 219.5 | 7 |

(a) According to the above table, complete the frequency distribution table in the ANSWER BOOKLET.
(b) Construct the frequency polygon in the ANSWER BOOKLET to represent the above data.

## Do not write on this page.

Answers written on this page will not be marked.
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## $\left.\mathbf{9} \mathbf{M}|\mathbf{E}| \mathbf{3} \left\lvert\, \begin{array}{l}\mathbf{(}\end{array}\right.\right)$

# Education Bureau <br> Territory-wide System Assessment 2023 

## Secondary 3 Mathematics ANSWER BOOKLET

## INSTRUCTIONS

1. Write your School Code, Class and Class Number in the boxes provided on this page.
2. Stick barcode labels in the spaces provided on page 1 and page 3 .
3. Time allowed is 65 minutes.
4. Write ALL your answers in the spaces provided in this ANSWER BOOKLET.
5. Do not write in the margins.
6. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
7. The use of HKEAA approved calculators is permitted.
8. Rough work should be done on the rough work sheet provided.


## SECTION A: Multiple Choice Questions

| MC Questions - Blacken the circle under the correct answer |
| :---: |
| with an HB pencil. For example : |
| A |
| A |

1. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
2. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
3. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
4. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
5. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
6. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
7. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
8. A B C D
$\bigcirc \bigcirc \bigcirc$
9. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C} D$
$\bigcirc \bigcirc \bigcirc$
10. A B C D
$\bigcirc \bigcirc \bigcirc$

Please stick the barcode label in the box. $\longrightarrow$
Please do not write in the margin.
11. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
12. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
13. A B C D
$\bigcirc \bigcirc \bigcirc$
14. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
15. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
16. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
17. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
18. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
19. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
20. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$

SECTION B: Write your answers in the spaces provided. Working need not be shown.
21. $\qquad$
22. $\qquad$
23.

24. The discount of the cake is $\qquad$ .
25. The value of the 3 rd term of the sequence is $\qquad$ .
26. $\qquad$
27. $\qquad$
28. $\qquad$
29. $c=$ $\qquad$
30. $\qquad$
31. $x=$ $\qquad$
32. $x=$ $\qquad$
33. $x=$ $\qquad$
34.
35. $P Q=$ $\qquad$ units
36. $x=$ $\qquad$
37.

| Table 1 |  |
| :---: | :---: |
| Number of vehicles <br> per minute | Frequency |
| $0-14$ |  |
| $15-29$ | 6 |
| $30-44$ |  |


| Table 2 |  |
| :---: | :---: |
| Number of vehicles <br> per minute | Frequency |
| $0-8$ |  |
| $9-17$ | 2 |
| $18-26$ |  |
| $27-35$ | 2 |
| $36-44$ |  |

38. (a) $\qquad$ batteries have been examined in the test.
(b) The median of the lifetime of batteries is $\qquad$ hours in the test.
(c) $\qquad$ batteries do not meet the requirement in the test.
39. The weighted mean score of Simon is $\qquad$ .

## SECTION C: Answer in the spaces provided. <br> All working and conclusions must be clearly shown.

40. $\qquad$
41. 

$2 x-y+1=0$

| $x$ | -3 | 0 | 2 |
| :---: | :---: | :---: | :---: |
| $y$ |  | 1 |  |


42. $\qquad$

46. $\qquad$
47. (a)

| Weight (g) | Class Mark (g) | Frequency |
| :---: | :---: | :---: |
| $150-169$ | 159.5 | 7 |
| $170-189$ | 179.5 | 6 |
| $190-209$ | 199.5 |  |
| $210-229$ | 219.5 | 7 |

(b)
Weight of 24 tomatoes


## END OF PAPER

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2023-TSA-MATH-9ME3(A)-8

## $\mathbf{9} \mathbf{M E} \mathbf{4}$ ( $\mathbf{Q}$ )

## Education Bureau

Territory-wide System Assessment 2023

## Secondary 3 Mathematics QUESTION BOOKLET

## INSTRUCTIONS

1. There are 47 questions in this paper.
2. Time allowed is 65 minutes.
3. Answer ALL questions in the separate ANSWER BOOKLET.
4. The use of HKEAA approved calculators is permitted.
5. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
6. Rough work should be done on the rough work sheet provided.
7. The diagrams in this paper are not necessarily drawn to scale.

SECTION A: Choose the best answer for each question. You should mark all your answers in the ANSWER BOOKLET.

1. Find the greatest common divisor $(\mathrm{gcd})$ of $2^{2} \times 3$ and $2 \times 3^{2} \times 5$.
A. $2 \times 3$
B. $2 \times 3 \times 5$
C. $2^{2} \times 3^{2} \times 5$
D. $2^{3} \times 3^{3} \times 5$
2. $x^{2}-y^{2}=$
A. $2 x-2 y$.
B. $x \cdot x-y \cdot y$.
C. $(x-y)^{2}$.
D. $x \cdot x+y \cdot y$.
3. Which of the following may represent the graph of the equation $x+y-7=0$ ?
A.

B.

C.

D.

4. $A(3,-4)$ and $B(9,-2)$ are two points in the rectangular coordinate plane. The coordinates of the mid-point of $A B$ are
A. $(12,-6)$.
B. $(6,-3)$.
C. $(3,1)$.
D. $(-3,-1)$.
5. Nancy and Ivan weigh $x \mathrm{~kg}$ and $y \mathrm{~kg}$ respectively. Their total weight is 70 kg . 3 times Nancy's weight equals 2 times Ivan's weight. Which of the following pairs of simultaneous equations shows the relation between $x$ and $y$ ?
A. $\left\{\begin{array}{l}x+y=70 \\ 2 x=3 y\end{array}\right.$
B. $\left\{\begin{array}{l}x+y=70 \\ 3 x=2 y\end{array}\right.$
C. $\left\{\begin{array}{l}2 x+3 y=70 \\ 2 x=3 y\end{array}\right.$
D. $\left\{\begin{array}{l}3 x+2 y=70 \\ 3 x=2 y\end{array}\right.$
6. Use a scientific notation to represent 0.00000012 .
A. $0.12 \times 10^{-6}$
B. $0.12 \times 10^{-7}$
C. $1.2 \times 10^{-6}$
D. $1.2 \times 10^{-7}$
7. Which of the following is NOT a polynomial?
A. $3+\frac{2}{y^{2}}$
B. $3+\frac{y^{2}}{2}$
C. $3+2 y$
D. $3+2 y^{2}$
8. $a(3 a+b-1)=$
A. $4 a+b-1$.
B. $4 a+a b-a$.
C. $3 a^{2}+a b-a$.
D. $3 a^{2}+b-1$.
9. Which of the following is an identity?
A. $x-3=3-x$
B. $2(x-3)=2 x-3$
C. $(x-3)(x+3)=x^{2}-9$
D. $(x+3)^{2}=x^{2}+9$
10. If $x \leq y$, which of the following inequalities is correct?
A. $\frac{x}{3} \geq \frac{y}{3}$
B. $3 x \geq 3 y$
C. $-3 x \leq-3 y$
D. $x-3 \leq y-3$
11. The figure shows a sphere. Its radius is 9 cm . Find the volume of the sphere.

A. $2 \pi(9)^{2} \mathrm{~cm}^{3}$
B. $4 \pi(9)^{2} \mathrm{~cm}^{3}$
C. $\frac{1}{3} \pi(9)^{3} \mathrm{~cm}^{3}$
D. $\frac{4}{3} \pi(9)^{3} \mathrm{~cm}^{3}$
12. The figure shows a solid right circular cone. Its height is 9 cm . Its base radius is 12 cm and its slant height is 15 cm . Find the total surface area of the cone.

A. $\pi(12)(15) \mathrm{cm}^{2}$
B. $\frac{1}{3} \pi(12)^{2}(9) \mathrm{cm}^{2}$
C. $\left[\pi(12)(15)+\pi(12)^{2}\right] \mathrm{cm}^{2}$
D. $\pi(12)^{2}(9) \mathrm{cm}^{2}$
13. Which of the following represents the rhombus in the figure?
A. PQRS
B. $\triangle P Q R$
C. $P R$
D. $P$

14. Which of the following figures MUST be a regular polygon?
A.
B.
C.
D.

15. In the figure, which point can be represented by $(-2,5)$ ?
A. $P$
B. $Q$
C. $R$
D. $S$

16. Which of the following points lies on the straight line $y=9 x+3$ ?
A. $(0,3)$
B. $(3,0)$
C. $(-1,6)$
D. $(1,-6)$
17. It is given that the slope of a straight line $\ell$ is $-\frac{1}{6}$. Which of the following straight lines is parallel to $\ell$ ?

| Line | $L_{1}$ | $L_{2}$ | $L_{3}$ | $L_{4}$ |
| :---: | :---: | :---: | :---: | :---: |
| Slope | 6 | -6 | $\frac{1}{6}$ | $-\frac{1}{6}$ |

A. $L_{1}$
B. $L_{2}$
C. $L_{3}$
D. $L_{4}$
18. Find the value of $\tan \theta$ in the figure.
A. $\frac{20}{29}$
B. $\frac{21}{29}$
C. $\frac{20}{21}$
D. $\frac{21}{20}$

19. Carmen applied for admission to a secondary school. The table below shows the weights of the admission criterion and her marks in these areas.

|  | Admission Criterion |  |  |
| :---: | :---: | :---: | :---: |
|  | Interview | Learning <br> Portfolio | Extra-Curricular <br> Activity |
| Mark | 70 | 80 | 90 |
| Weight | 5 | 3 | 2 |

Find the weighted mean mark of Carmen.
A. 24
B. 77
C. 80
D. 240
20. The following table shows the service status of trains and their corresponding frequency at a station yesterday.

| Service status | Left ahead of time | Left on time | Left behind schedule |
| :---: | :---: | :---: | :---: |
| Frequency | 0 | 1997 | 3 |

Find the relative frequency of the service status "left behind schedule" at the station yesterday.
A. 0
B. $\frac{1997}{2000}$
C. $\frac{3}{2000}$
D. $\frac{3}{1997}$

## SECTION B: Write ALL the answers in the ANSWER BOOKLET.

 Working need not be shown.21. Use powers to express $5 \times 5 \times 5$.
22. Write down the numbers represented by $A, B$ and $C$ on the number line below.

23. Round off 381500 to 3 significant figures.
24. The marked price of a cake is $\$ 320$. If it is sold at $30 \%$ off, find the discount.
25. A box contains 20 jelly candies. 8 of them are orange in colour and the rest are yellow. Find the ratio of the number of orange jelly candies to that of yellow jelly candies.
26. Simplify $(3 x-7)+(8-3 x)$.
27. Expand $(x-1)(x+5)$.
28. Expand $(-x+4)(-3 x)$.
29. Factorise $x^{2}+12 x+36$.
30. Simplify $\frac{1}{2 x}+\frac{2}{x}$.
31. According to the diagram, write down an inequality in $x$.

32. Alice runs around the park. She takes 80 seconds (correct to the nearest second) to finish a lap. Find the percentage error of the measured value.
33. The figure shows a pentagon $A B C D E$ and its exterior angles. Find $x$.

34. 



In the figure, $\triangle A B C \sim \triangle A D E$. Find
(a) the value of $x$,
(b) the value of $y$.
35. In the figure, $A B C D$ is a parallelogram. It is given that $\angle A D C=130^{\circ}$. Find $x$.

36. In the figure, $\boldsymbol{Q}(-3,2)$ is translated downwards by 2 units to $\boldsymbol{Q}^{\prime}$. Find the coordinates of $\boldsymbol{Q}^{\prime}$.

37. The following data shows the average traffic flow (number of vehicles per minute) of a location in last 15 days.

| 42 | 20 | 5 | 30 | 12 |
| :---: | :---: | :---: | :---: | :---: |
| 44 | 40 | 36 | 22 | 24 |
| 33 | 38 | 16 | 18 | 24 |

Use the data to complete the two frequency distribution tables in the ANSWER BOOKLET.
38. The cumulative frequency curve below shows the result of the lifetime of some batteries in a test.


According to the cumulative frequency curve shown above, answer the following questions.
(a) How many batteries have been examined in the test?
(b) Find the median of the lifetime of batteries in the test.
(c) If the lifetime of a battery is not more than 2 hours, its quality does not meet the requirement. How many batteries do not meet the requirement in the test?
39. The table below shows the amount of "Consumption Voucher" spent by 36 people within the first week.

| Amount Spent (dollar) | $1-1000$ | $1001-2000$ | $2001-3000$ | $3001-4000$ | $4001-5000$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of people | 2 | 6 | 11 | 2 | 15 |

Find the modal class of the amount of "Consumption Voucher" spent by the 36 people.

SECTION C: All working must be clearly shown.
Write the mathematical expressions, answers and statements/conclusions in the spaces provided in the ANSWER BOOKLET.
40. Peter exchanges 86000 Japanese Yen in a bank for Hong Kong dollars. The exchange rate is 100 Japanese Yen to 6.5 Hong Kong dollars. Find the amount in Hong Kong dollars he should receive.
41. Complete the table for the equation $y=2 x+1$ in the ANSWER BOOKLET.

| $x$ | -3 | 0 | 2 |
| :--- | :--- | :--- | :--- |
| $y$ |  | 1 |  |

According to the table, plot the graph of this equation on the rectangular coordinate plane given in the ANSWER BOOKLET.
42. In the figure, $A C D$ is a straight line. $\angle B A D=45^{\circ}$ and $\angle B C D=3 x-75^{\circ}$. Find $x$.

43. In the figure, $A E C$ and $D E B$ are straight lines. $\angle B A E=\angle C D E$ and $A E=D E$. Prove that $\triangle A B E \cong \triangle D C E$.

44. In the figure, $A B C D$ is a rhombus. $A C$ and $B D$ are perpendicular to each other and they intersect at point $E$. It is given that $A E=7 \mathrm{~cm}$ and $B E=2.4 \mathrm{~cm}$. Find the perimeter of the rhombus.

45. Find the area of $\triangle A B C$ in the figure.

46. The table below shows the results of 3 A students in a Mathematics competition.

| Result (mark) | $1-20$ | $21-40$ | $41-60$ | $61-80$ | $81-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 5 | 8 | 12 | 4 | 1 |

(a) According to the above table, complete the frequency distribution table in the ANSWER BOOKLET.
(b) Find the mean of the Mathematics competition results of 3A students.
47. A dessert shop offers three flavours of shaved ice including watermelon (W), strawberry (S) and chocolate (C). Each portion of shaved ice can have one topping of nuts (N), marshmallows (M) or biscuit (B).
(a) Some of the possible outcomes are given in the table provided in the ANSWER BOOKLET. Fill the rest of the possible outcomes in the blanks.
(b) If Kelvin chooses a shaved ice flavour and a topping randomly, find the probability that he chooses watermelon shaved ice with nuts.

END OF PAPER

## Do not write on this page.

Answers written on this page will not be marked.
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Prepared by the Hong Kong Examinations and Assessment Authority

## $\left.\begin{array}{l|l|l|l|l|l}\mathbf{9} & \mathbf{M} & \mathbf{E} & \mathbf{4} & \mathbf{(} & \mathbf{A}\end{array}\right)$

# Education Bureau <br> Territory-wide System Assessment 2023 

## Secondary 3 Mathematics ANSWER BOOKLET

## INSTRUCTIONS

1. Write your School Code, Class and Class Number in the boxes provided on this page.
2. Stick barcode labels in the spaces provided on page 1 and page 3 .
3. Time allowed is 65 minutes.
4. Write ALL your answers in the spaces provided in this ANSWER BOOKLET.
5. Do not write in the margins.
6. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
7. The use of HKEAA approved calculators is permitted.
8. Rough work should be done on the rough work sheet provided.


## SECTION A: Multiple Choice Questions

| MC Questions - Blacken the circle under the correct answer |
| :---: |
| with an HB pencil. For example : |
| A |
| A |

1. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
2. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
3. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C}$
$\bigcirc \bigcirc \bigcirc \bigcirc$
4. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
5. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
6. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
7. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
8. A B C D
$\bigcirc \bigcirc \bigcirc$
9. $\mathrm{A} \quad \mathrm{B} \quad \mathrm{C} D$
$\bigcirc \bigcirc \bigcirc$
10. A B C D
$\bigcirc \bigcirc \bigcirc$

Please stick the barcode label in the box. $\longrightarrow$
Please do not write in the margin.
11. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
12. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
13. A B C D
$\bigcirc \bigcirc \bigcirc$
14. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
15. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
16. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
17. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
18. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
19. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$
20. A B C D
$\bigcirc \bigcirc \bigcirc \bigcirc$

SECTION B: Write your answers in the spaces provided. Working need not be shown.
21. $\qquad$
22. $A=$ $\qquad$
$B=$ $\qquad$
$C=$ $\qquad$
23. $\qquad$
24. The discount of the cake is $\qquad$ .
25. Number of orange jelly candies : Number of yellow jelly candies $=$ $\qquad$ : $\qquad$
26. $\qquad$
27. $\qquad$
28. $\qquad$
29. $\qquad$
30. $\qquad$
31. $\qquad$
32. The percentage error of the measured value is $\qquad$ .
33. $x=$ $\qquad$
34. (a) $x=$ $\qquad$
(b) $y=$ $\qquad$
35. $x=$ $\qquad$
36. The coordinates of $\boldsymbol{Q}^{\prime}$ are ( $\qquad$ , $\qquad$ ).
37.

| Table 1 |  |
| :---: | :---: |
| Number of vehicles <br> per minute | Frequency |
| $0-14$ |  |
| $15-29$ | 6 |
| $30-44$ |  |


| Table 2 |  |
| :---: | :---: |
| Number of vehicles <br> per minute | Frequency |
| $0-8$ |  |
| $9-17$ | 2 |
| $18-26$ |  |
| $27-35$ | 2 |
| $36-44$ |  |

38. (a) $\qquad$ batteries have been examined in the test.
(b) The median of the lifetime of batteries is $\qquad$ hours in the test.
(c) $\qquad$ batteries do not meet the requirement in the test.
39. The modal class of the amount of "Consumption Voucher" spent by the 36 people is $\$$ $\qquad$ - \$ $\qquad$ .
SECTION C: Answer in the spaces provided. All working and conclusions must be clearly shown.
40. 


41.
$y=2 x+1$

| $x$ | -3 | 0 | 2 |
| :---: | :---: | :---: | :---: |
| $y$ |  | 1 |  |


42.

43.

44.

45.

46. (a)

| Result (mark) | $1-20$ | $21-40$ | $41-60$ | $61-80$ | $81-100$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Class Mark (mark) | 10.5 |  | 50.5 |  | 90.5 |
| Frequency | 5 | 8 | 12 | 4 | 1 |

(b)
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
47. (a)

| (a) |  |  |  |  | Shaved ice |  |  |
| :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: |
|  | Watermelon (W) |  |  |  | Strawberry (S) | Chocolate (C) |  |
| Topping | Nuts (N) | NW |  |  |  |  |  |
| Marshmallows (M) | MW | MS |  |  |  |  |  |
|  | Biscuit (B) |  | BS |  |  |  |  |

(b) The probability that Kelvin chooses watermelon shaved ice with nuts $=$ $\qquad$
END OF PAPER
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